



# ClassifierEnsembles: Select real-world applications

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#### Contenidos

- 1. Objective of the article
- 2. Introduction to classifier ensembles
- 3. Classifier ensemble methods
- 4. Real-World applications
- 5. Conclusions









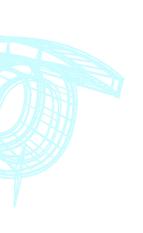
## **Objective of the article**

- \* Introduce classifier ensembles
  - Definitions
    - Classifier ensembles
    - Bias/Variance tradeoff
    - Bayesian interpretation
  - ☐ Summarize leading ensemble methods
    - Simple averaging
    - Weighted averaging
    - Stacking
    - Bagging
    - Boosting
    - Order statistics
- Show real-word applications, in 4 different domains:
  - Remote sensing
  - Person recognition
  - ☐ One vs. all recognition
  - Medicine













- \* Classification task:
  - Requires the construction of a statistical model that represents a mapping from input data to the appropriate outputs.
  - Model: intended to approximate the true mapping from the inputs to the outputs
  - Purpose: generate predictions of outputs for new, previously unseen inputs.
- \* Single classifier to make predictions for new examples.
  - BUT: many decisions affect the performance of that classifier.
  - ☐ Option A: selecting the best available classifier
    - BUT: distribution over new examples that the classifier may encounter during operation may vary
    - BUT: many classifiers are generally tried before a single classifier is selected.
       Therefore, valuable information discarded by ignoring the performance of all the other classifiers.
  - ☐ Option B: Classifier ensembles





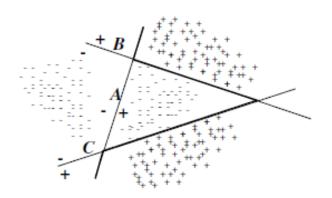






Classifier ensembles (combiners or committees)

- \* Aggregations of several classifiers whose individual predictions are combined in some manner (e.g., averaging or voting) to form a final prediction.
- ★ Use all the available classifier information
  - ☐ Generally provide better and/or more robust solutions in most applications



#### Example:

An ensemble of linear classifiers (boldface line). Each line A, B, and C is a linear classifier.









#### Bias vs variance

- ☐ Bias = Difference between the true function that generated the data and the "average" function returned by the learning algorithm
  - Averaged over all possible training sets
  - Question: Average of {house, car, house, shoe, house, house} ?
- □ Variance over the possible training sets of the function returned by the learning algorithm
- Simpler model: bias  $\uparrow$ , variance  $\downarrow$











- Bayesian interpretation
  - ☐ Ensemble learning: tractable approximation to full bayesian learning
  - Bayesian learning:
    - Final learned model is mixture of very large set of models (eg. All models in a given family):

$$P(Y|T) = \sum_{m=1}^{M} P(Y|h_m)P(h_m|T)$$

$$= \sum_{m=1}^{M} P(Y|h_m) \frac{P(T|h_m)P(h_m)}{P(T)}.$$

- Predict some quantity Y
- Set of models (large M)  $h_m \ (m \in \{1, 2, \ldots, M\}$
- Training set T

**Approximation**: using mixture of a small set of models having

- **Highest** posterior probabilities  $P(h_m|T)$
- **Highest** likelihoods  $P(T|h_m)$









#### **Classifier ensemble methods**

- \* Simple averaging
- ★ Weighted averaging
- \* Stacking
- \* Bagging
- \* Boosting
- \* Order statistics











## Classifier ensemble methods - Simple averaging

If M classifiers  $(h_i^m(x), m)$ 

 $\in \{1, 2, ..., M\}$ ) are available, the class  $C_i$  output of the averaging combiner is:

$$h_i^{\text{ave}}(x) = \frac{1}{N} \sum_{m=1}^M h_i^m(x)$$
 (1)

#### \* Benefits

- Reduces the variance of the estimate of the output class posteriors
- ☐ Simple: widely applied to real-world problems
- ☐ Effective ensemble method, particularly in large complex data

#### \* Problems

Reduces model error

$$E_{\text{model}}^{\text{ensemble}} = \frac{1 + \rho(M - 1)}{M} E_{\text{model}}$$

ho: Average correlation among the errors of the different classifiers









# Classifier ensemble methods - Weighted averaging

★ Different classifier weight

$$h_i^{\text{ave}}(x) = \frac{1}{M} \sum_{m=1}^M w_m h_i^m(x)$$



- \* But in practice
  - ☐ failed to provide improvement to justify its added complexity
  - When there is limited training data with which the weights can be properly estimated









### **Classifier ensemble methods - Stacking**

- \* Actively seeks to improve the performance of the ensemble by correcting the errors
- \* Stacked generalization addresses the issue of classifier bias with respect to a training set, and aims at learning and using these biases to improve classification
- \* The main concept is to use a new classifier to correct the errors of a previous classifier











#### **Classifier ensemble methods - Bagging**

- Bootstrapped Aggregating (Bagging)
  - □ Combines voting with a method for generating the classifiers that provide the votes
  - Allow each base classifier to be trained with a different random subset of the patterns with the goal of bringing about diversity in the base classifiers.
- improve upon their base models more if the base model learning algorithms are unstable (ej. Decision trees)
  - differences in their training sets tend to induce significant differences in the models













#### **Classifier ensemble methods - Bagging**

Bootstrapped Aggregating (Bagging)

```
\begin{aligned} \mathbf{Bagging}(T, M) \\ & \text{For each } m = 1, 2, \dots, M, \\ & T_m = Sample\_With\_Replacement(T, |T|) \\ & h_m = L_b(T_m) \\ & \text{Return } h_{fin}(x) = \operatorname{argmax}_{y \in Y} \sum_{m=1}^M I(h_m(x) = y) \end{aligned}
\begin{aligned} \mathbf{Sample\_With\_Replacement}(T, N) \\ & S = \emptyset \\ & \text{For } i = 1, 2, \dots, N, \\ & r = random\_integer(1, N) \\ & \text{Add } T[r] \text{ to } S. \end{aligned}
\text{Return } S.
```







#### **Classifier ensemble methods - Boosting**

- ★ AdaBoost algoritm
  - ☐ Generates a sequence of base models with different weight distributions over the training set

AdaBoost(
$$\{(x_1, y_1), \dots, (x_N, y_N)\}, L_b, M$$
)  
Initialize  $D_1(n) = 1/N$  for all  $n \in \{1, 2, \dots, N\}$ .  
For  $m = 1, 2, \dots, M$ :  
 $h_m = L_b(\{(x_1, y_1), \dots, (x_N, y_N)\}, D_m)$ .  
Calculate the error of  $h_m : \epsilon_m = \sum_{n:h_m(x_n) \neq y_n} D_m(n)$ .  
If  $\epsilon_m \geq 1/2$  then,  
set  $M = m - 1$  and abort this loop.  
Update distribution  $D_m$ :

$$D_{m+1}(n) = D_m(n) \times \begin{cases} \frac{1}{2(1-\epsilon_m)} & \text{if } h_m(x_n) = y_n \\ \frac{1}{2\epsilon_m} & \text{otherwise} \end{cases}$$

Output the final model:

$$h_{fin}(x) = \operatorname{argmax}_{y \in Y} \sum_{m:h_m(x)=y} log \frac{1-\epsilon_m}{\epsilon_m}$$
.





#### Classifier ensemble methods - Order statistics

- Order statistics combiners that selectively pick a classifier on a per sample basis
- \* Model error

$$E_{\text{model}}^{\text{ensemble}} = \alpha E_{\text{model}}$$

□ Alpha is a factor that depends on the number of classifiers M and the order statistic chosen and the error model

M	OS combiners	
	min/max	med
1	1.000	1.000
2	0.682	0.532
3	0.560	0.449
4	0.492	0.305
5	0.448	0.287
10	0.344	0.139
15	0.301	0.102
20	0.276	0.074





## **Real-world applications**

- \* Remote sensing
- \* Person recognition
- \* One vs. all recognition
- \* Medicine









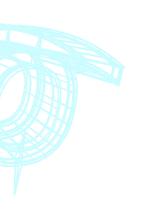


## Real-world applications - Remote sensing

- \* Classification algorithms needs
  - □ large number of inputs
    - patterns collected repeatedly for large spaces
  - □ large number of features
    - data is collected across hundreds of bands
  - □ large number of outputs
    - classes cover many types of terrain (forest, agricultural area, water) and manmade objects (houses, streets)
  - missing or corrupted data
    - different bands or satellites may fail to collect data at certain times
  - poorly labeled (or unlabeled) data
    - data needs to be post-processed and assigned to classes











## Real-world applications - Remote sensing

- \* Example applications
  - Random forests and mountainous terrain
  - Majority voting for agricultural land
  - Hierarchical classification of wetlands
  - Information fusion for Urban areas











## Real-world applications – Person recognition

- \* Person recognition is the problem of verifying the identity of a person using characteristics of that person, typically for security applications
  - Iris recognition
  - fingerprint recognition
  - ☐ face recognition
  - behavior recognition
    - such as speech and handwriting
    - recognizing characteristics of a person, as opposed to depending upon specific knowledge that the person may have (such as usernames and passwords for computer account access)
- \* Problems
  - ☐ Involve multiple types of features
  - Difficulty in collecting good data
  - Different misclassification costs
    - Example, denying system access to a legitimate user vs. allowing access to an illegitimate user





## Real-world applications - Person recognition

- \* Example applications
  - ☐ Unobtrusive person identification
  - ☐ Face recognition
  - Multi-modal person recognition
  - User-specific speech recognition













## Real-world applications - One vs. all recognition

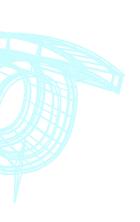
#### ★ Different types

- Anomaly detection
  - problem of detecting unusual patterns
  - i.e. what does not fit into the set of identified patterns
- Target recognition
  - finding what fits into an identified pattern
- Intrusion detection
  - solved both ways:
  - A. target recognition: look for one of a set of known types of attacks
  - B. anomaly detection: look for anomalies in the usage patterns













## Real-world applications - One vs. all recognition

- \* Example applications
  - Modular intrusion detection
  - Hierarchical intrusion detection
  - Intrusion detection in mobile ad-hoc networks











## Real-world applications - Medicine

- \* Different applications:
  - analyzing X-ray images, human genome analysis, and examining sets of medical test data to look for anomalies.
  - Root of all these problems: assessing the health of human beings
- Characteristics
  - ☐ limited training and test examples
    - i.e., few training examples due to the nature of problem and privacy concerns
  - imbalanced datasets
    - ie., very few anomalies or examples of patients with a disease
  - too many attributes
    - i.e., often many more than the number of training and test examples
  - different misclassification costs
    - i.e., false negatives significantly worse than false positives.









# **Real-world applications - Medicine**

- \* Example applications
  - Pharmaceutical molecule classification
  - MRI classification
  - ECG classification











#### **Conclusions**

\* Each ensemble method has different properties that make it better suited to particular types of classifiers and applications



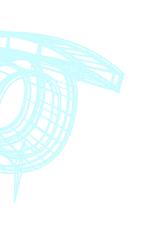
- New applications, domains with complex and rich data
- \* Research areas:
  - Ensemble methods oriented at handling large amounts of diverse data
  - Clustering algorithms
  - Distributed classifier ensembles using active/agent-based methods













**Gracias** 





