

# Contributions to Visual Servoing for legged and linked multicomponent robots

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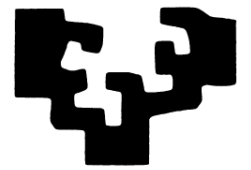
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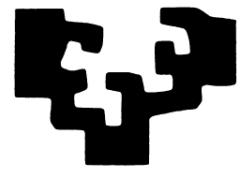
Dissertation presented for the degree of Doctor of Philosophy

2009



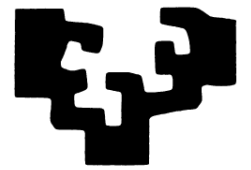
# Outline

- Introduction
- Visual Servoing general ideas
- Visual Servoing for legged robots
- Control of Linked MCRS
- Conclusion



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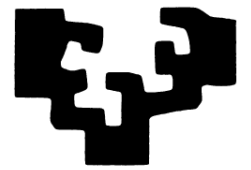
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# Introduction

## Motivation

- Vision has great importance in robotics since it allows to get a comprehensive description of the environment and is not an intrusive sensor.
- Visual Servoing systems define a direct relationship between vision and robot actuators.
- For legged robots we have found scarce literature on vision based control approaches.
- The Aibo robot is useful for research because it integrates a computer, vision system and articulators, being cheaper than the conventional robots for research.



# Introduction

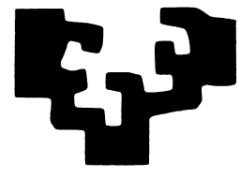
## Motivation

- MCRS offer the possibility to execute a task through the cooperation of a set of robot that a single robot could not execute.
- Linked MCRS is a new category that has not been explored.
- Vision is the most suitable sensor for determining the form of the hose, no other sensors are available.



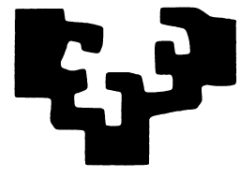
# Introduction

## Objectives



Develop applications of Visual Servoing to:

- Control of all the degrees of freedom of a legged robot.
- Control of Linked Multi-component Robots Systems.



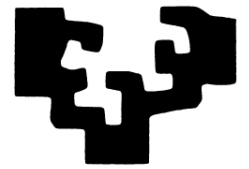
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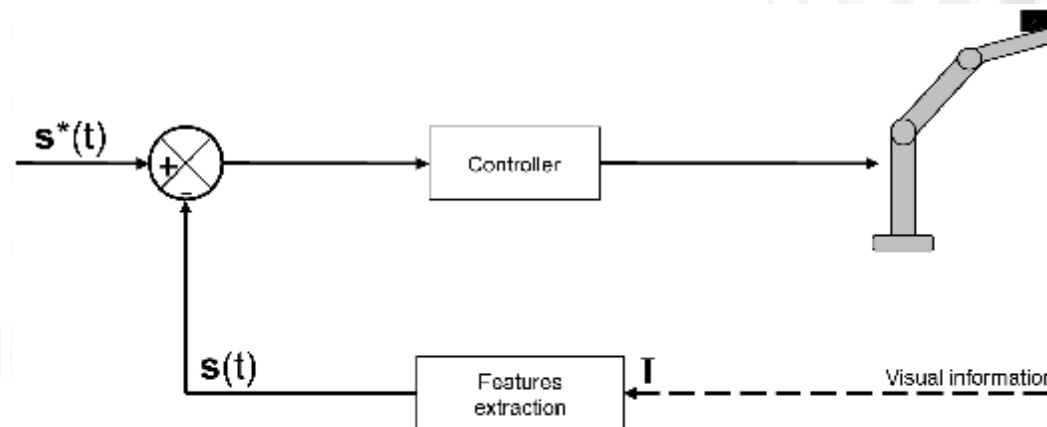
# Visual Servoing General Ideas

## Definition

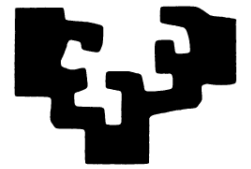


The task of positioning one or more robots in order to get poses of their final effectors using as feedback the visual information extracted by one or more video-cameras.

- For robotic manipulators: the pose of the final effector is relative to a target defined by a set of image features.
- For mobile robots: the pose is relative to some landmarks detected in the environment.





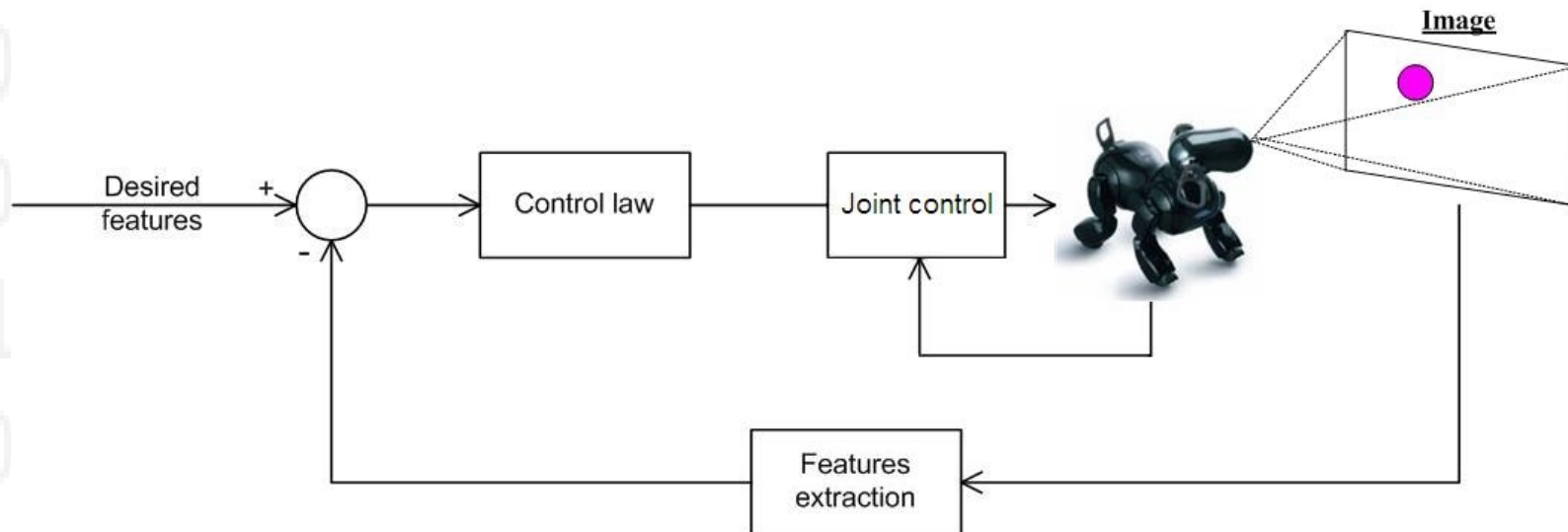
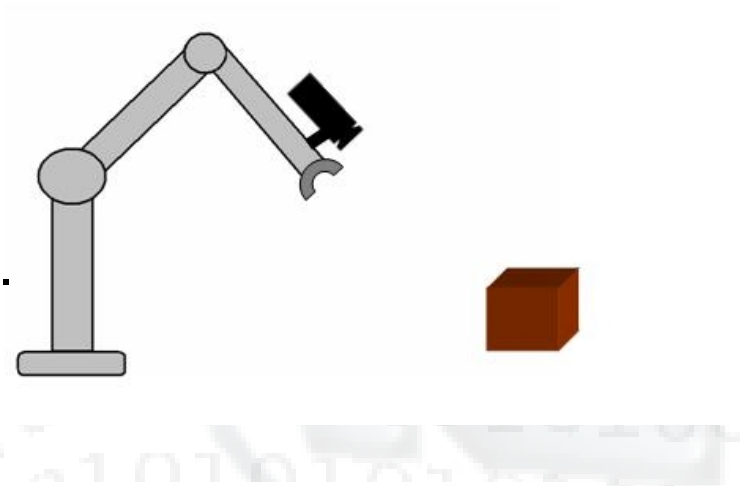


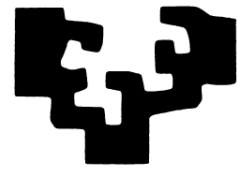
# Visual Servoing General Ideas

## Classification according to camera configuration

### Eye in hand

- Task is centered on the target object.
- Relation between poses of camera and robot's final effector is known and constant.
- Possibility of losing track of the target object.
- The camera intrinsic parameters may be required.



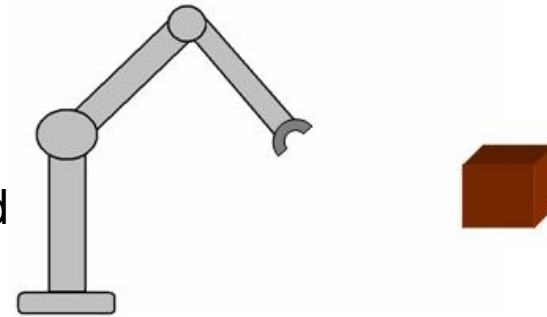


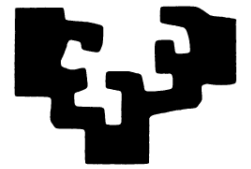
# Visual Servoing General Ideas

## Classification according to camera configuration

### Fixed camera

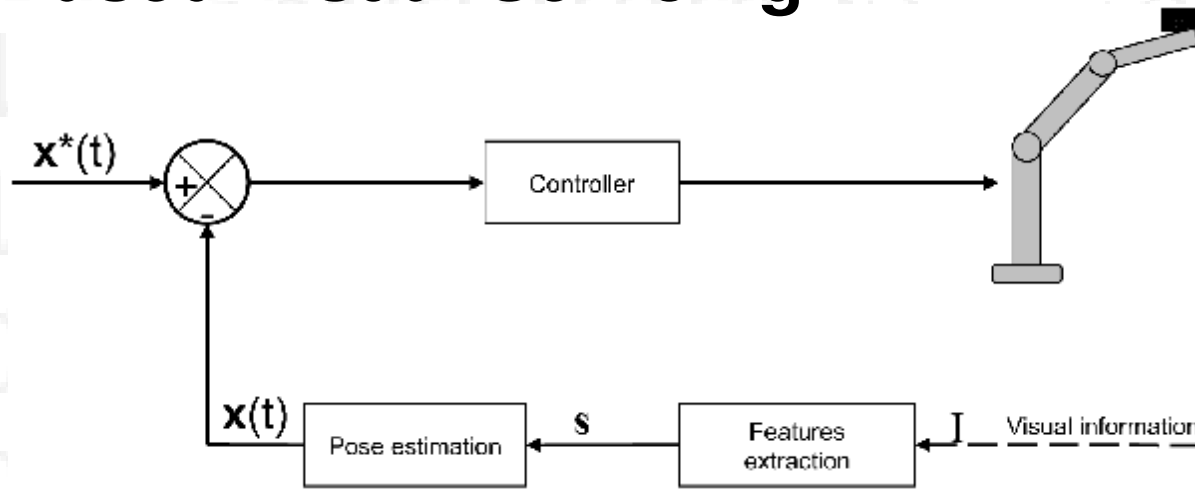
- Images of robots and the working space simultaneously.
- Fixed relationship between the camera reference system and the task reference system.
- Occlusions of the target object robots.
- It is necessary to calibrate the camera intrinsic and extrinsic parameters.





# Visual Servoing General Ideas Architectures

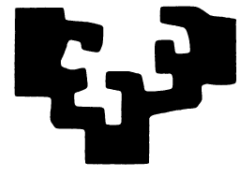
## Position Based Visual Servoing



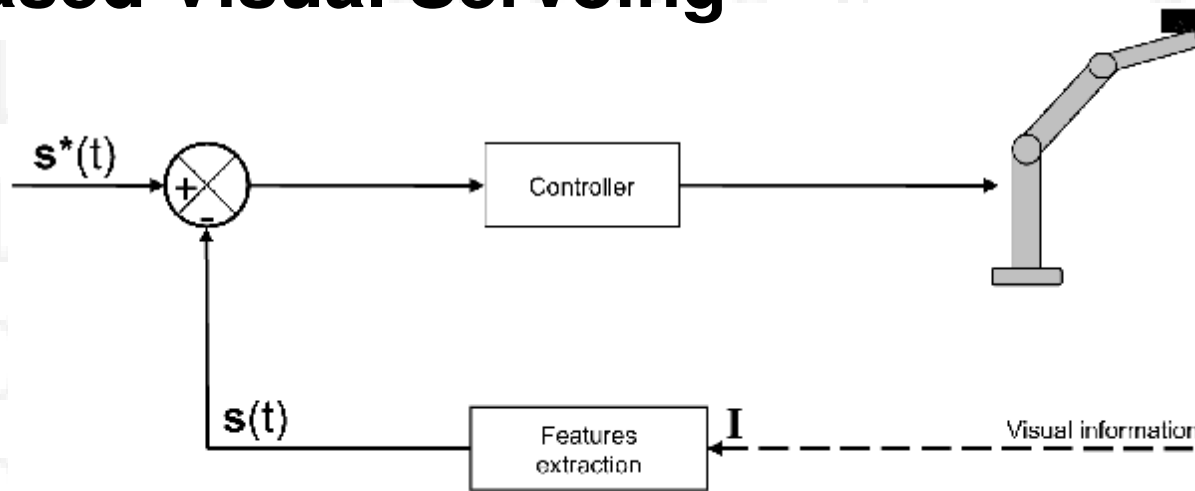
- The error signal is defined in the 3D space (the task space).
- Image features are extracted and used to estimate the pose through a tri-dimensional reconstruction of the environment's structure.



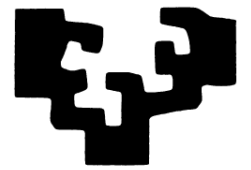
# Visual Servoing General Ideas Architectures



## Image Based Visual Servoing



- The error signal is defined in the bi-dimensional image reference system.
- Image features are used directly to control the robot joints (Image Jacobian matrix).

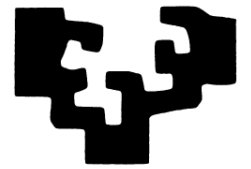


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  - Coordinate reference systems
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  - Inverse Kinematics
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# Visual Servoing for Legged robots



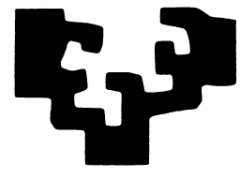
## Introduction

### **Motivation**

- Scarce Vision based control approaches for this kind of robots.
- Most of the approach only move the effectors linked directly to the camera or use high level control commands.



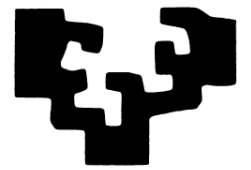
# Visual Servoing for Legged robots



## Introduction

### Objectives

- Build a detailed model of the image Jacobian matrix which formalizes a linear approach to the robot's kinematics.
- Taking into account all the effectors that can affect the image captured by the robot's camera.



# Outline

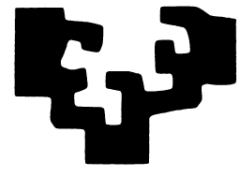
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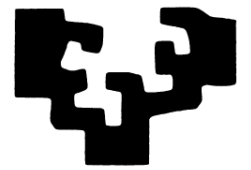


# Visual Servoing for Legged robots

## General description of the approach

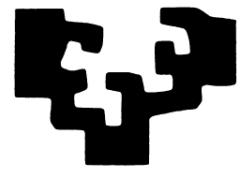


- For solving the system we follow the conventional lines of the Image Based Visual Servoing (IBVS) systems.
- We build a locally linear kinematic model of the robot by composing the diverse Jacobians matrices that embody the dependencies among observation and control parameters.
- We propose a simple inversion of the model to obtain the desired control commands that will accomplish the minimization of the perceptual error detected in the vision system.



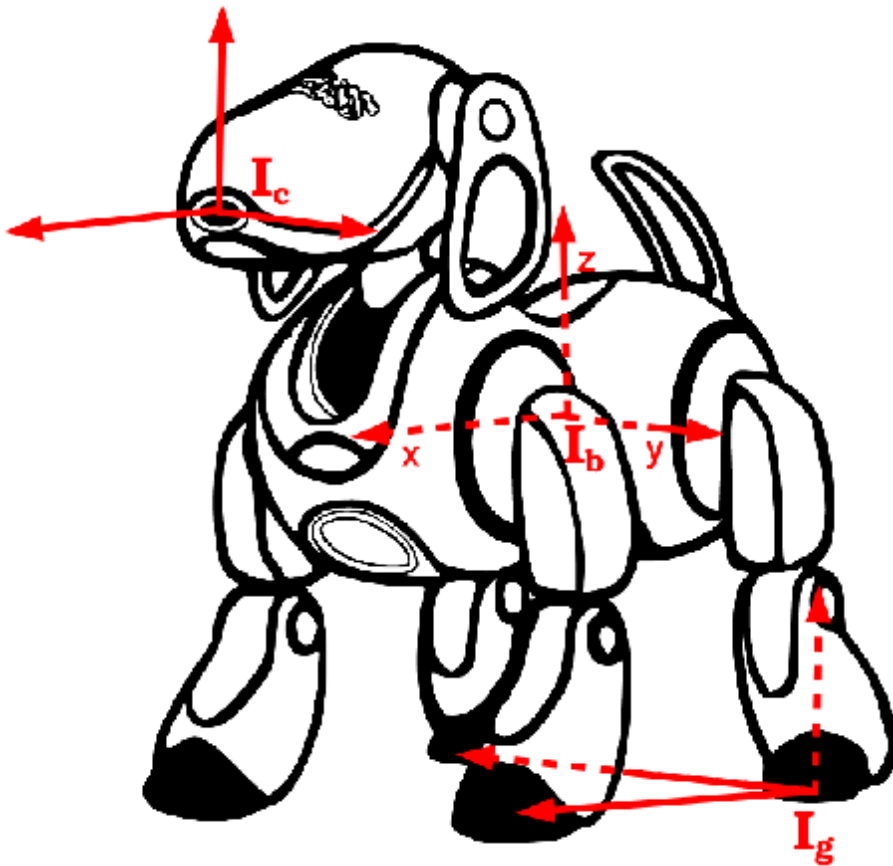
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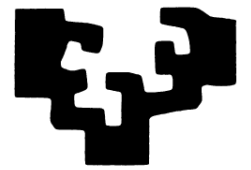


# Visual Servoing for Legged robots

## Coordinate reference systems



- Camera reference system
- Body reference system, whose origin is the geometrical center of the robot's body.
- Ground reference system, anchored to one of the basic ground support points defined later.



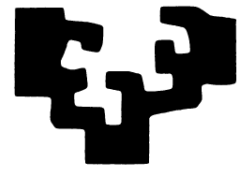
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# Visual Servoing for Legged robots

## Basic problems

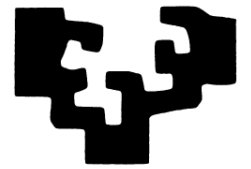


- 1) Determination of the ground plane.
- 2) Definition of a fixed ground reference system.



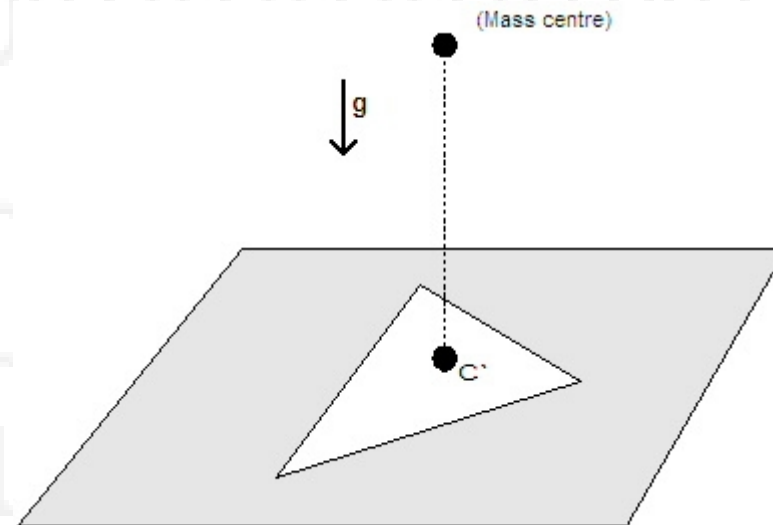
# Visual Servoing for Legged robots

## Basic problems



### 1. Determination of the ground plane.

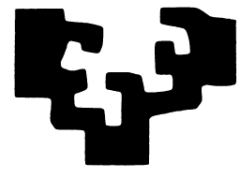
We use a gravity sensor and the joint state information provided by the robot's basic control systems.





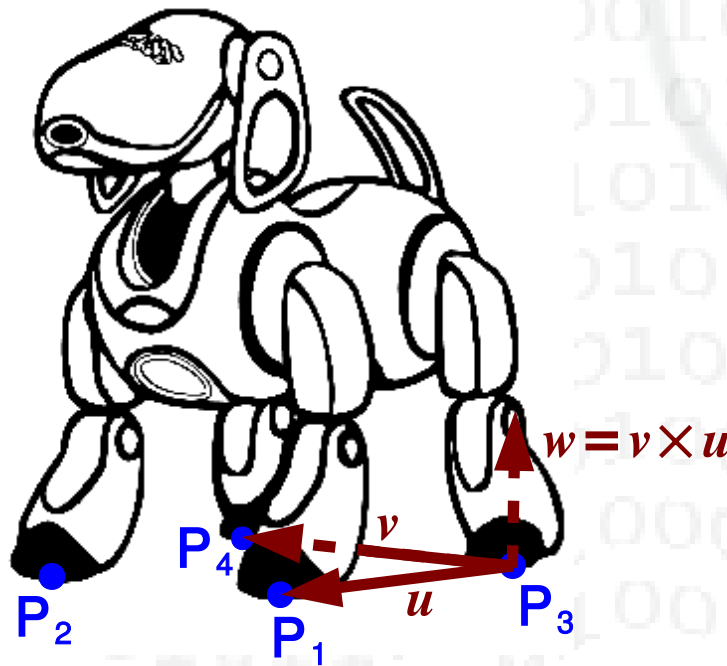
# Visual Servoing for Legged robots

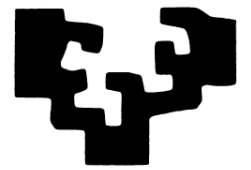
## Basic problems



### 2. Definition of a fixed ground reference system.

We use the tips of the legs for defining the ground reference system.

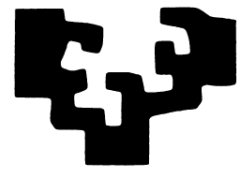




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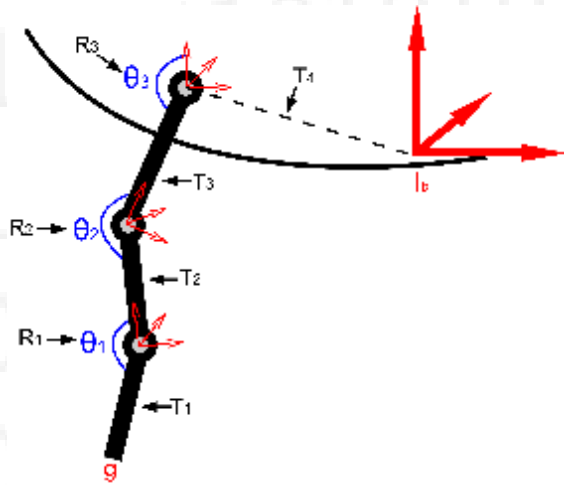




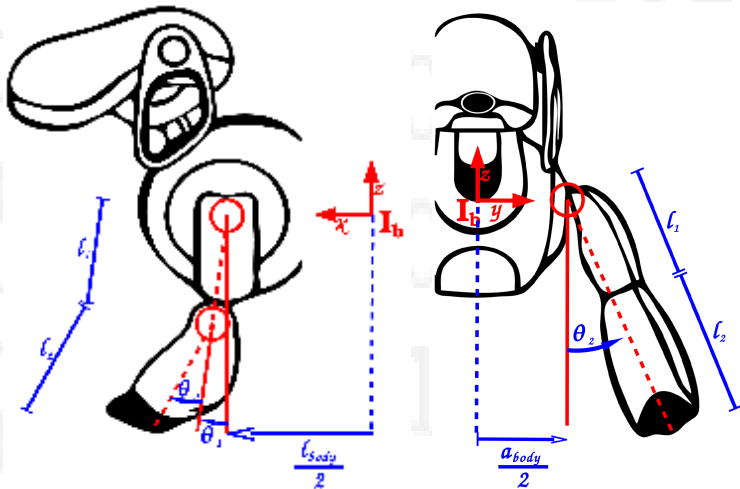
# Visual Servoing for Legged robots

## Direct Kinematics

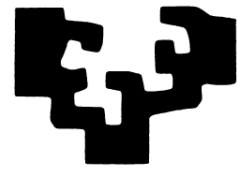
### Legs' degrees of freedom



$$\begin{pmatrix} g \\ 1 \end{pmatrix} = T_{n+1} \dots R_n \cdot T_n \dots R_1 \cdot T_1 \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$



$$\begin{pmatrix} x_p \\ y_p \\ z_p \\ 1 \end{pmatrix} = T_a \cdot T_b \cdot R_1 \cdot R_2 \cdot T_1 \cdot R_3 \cdot T_2 \begin{pmatrix} 0 \\ 0 \\ 0 \\ 1 \end{pmatrix}$$



# Visual Servoing for Legged robots

## Direct Kinematics

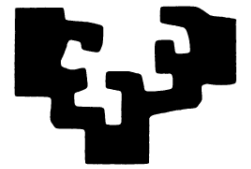
### Support points

The **basic support points** are the tips of the three legs that determine the supporting plane where it is standing on.

$$\mathbf{G}_\pi = \left( \mathbf{g}_1, \mathbf{g}_2, \mathbf{g}_3 \right)^t$$

The **extended support points** are the tips of the robot's legs that are in contact with the ground

$$\mathbf{G}_e = \left\{ \mathbf{g} \quad s.t. \quad |a \mathbf{g}_x + b \mathbf{g}_y + c \mathbf{g}_z| < tol \right\}$$



# Visual Servoing for Legged robots

## Direct Kinematics

### Vectors of parameters

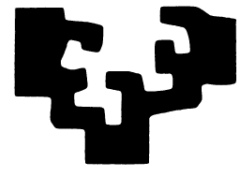
- We define the vectors of parameters as the composition of the upper articulations joint angles and the support points.

Basic parameter vector

$$\mathbf{p}_{\pi} = \begin{pmatrix} \boldsymbol{\theta}_u \\ \mathbf{G}_{\pi} \end{pmatrix}$$

Extended parameter vector

$$\mathbf{p} = \begin{pmatrix} \boldsymbol{\theta}_u \\ \mathbf{G}_e \end{pmatrix}$$

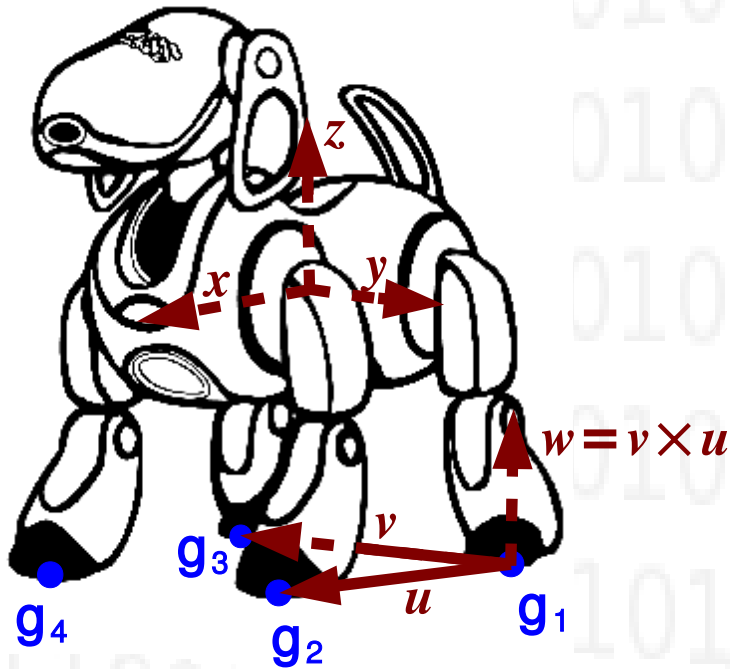


# Visual Servoing for Legged robots

## Direct Kinematics

### Transformation between ground and body systems

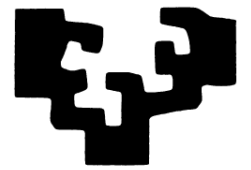
Legs degrees of freedom



$$R_0 = \begin{pmatrix} u & v & v \times u \\ 0 & 0 & 1 \end{pmatrix}$$

$$T_0 = \begin{pmatrix} I_{3 \times 3} & \mathbf{g}_1 \\ \mathbf{0} & 1 \end{pmatrix}$$

$${}_b I_g = T_0 \cdot R_0$$

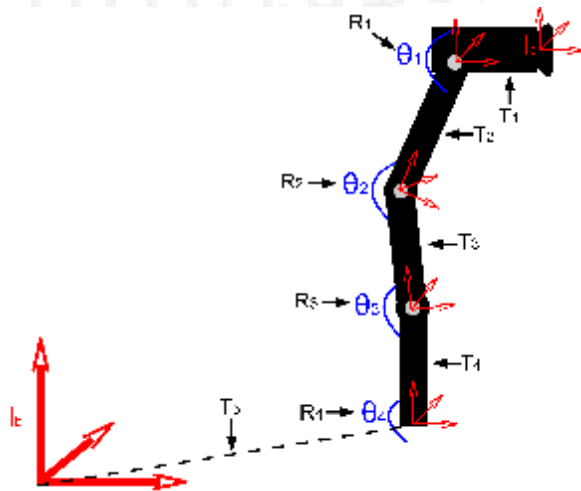


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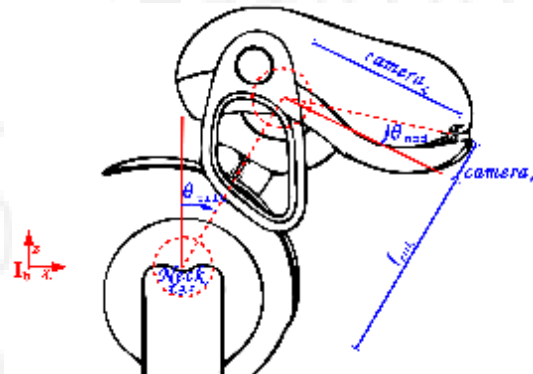
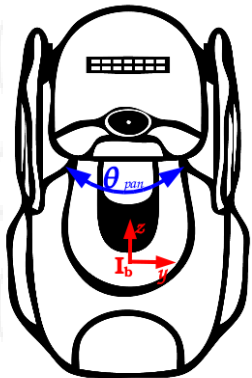
## Direct Kinematics

### Transformation between body and camera systems

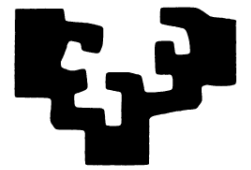
Upper body degrees of freedom



$${}^b I_c = (T_{m+1} \cdot R_m \cdot T_m \dots R_1 \cdot T_1)$$



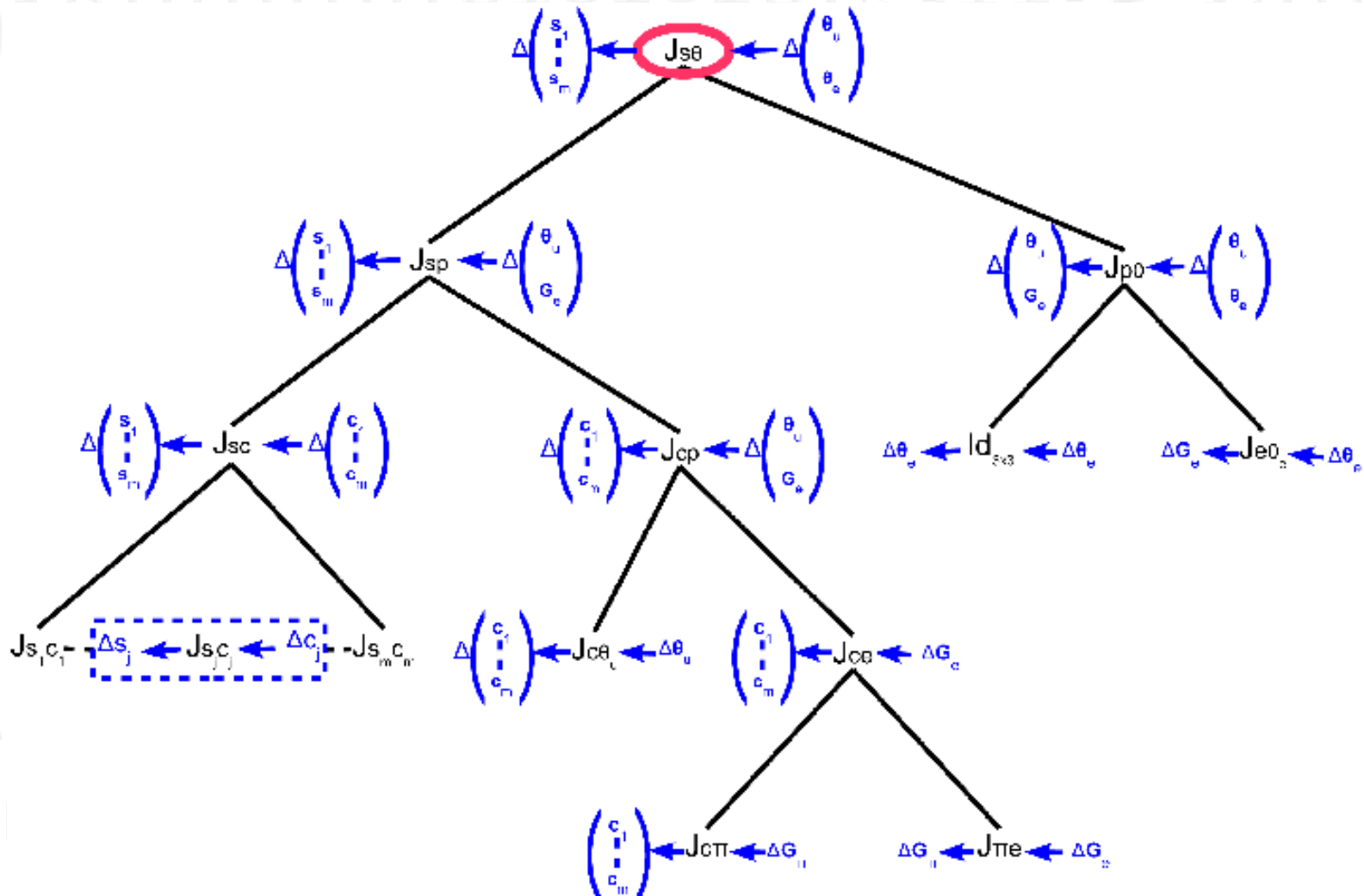
$${}^b I_c = (T_3 \cdot R_2 \cdot T_2 \cdot R_1 \cdot T_1)$$

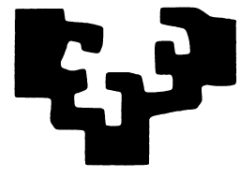


# Visual Servoing for Legged robots

## Direct Kinematics

Structure of direct kinematic function

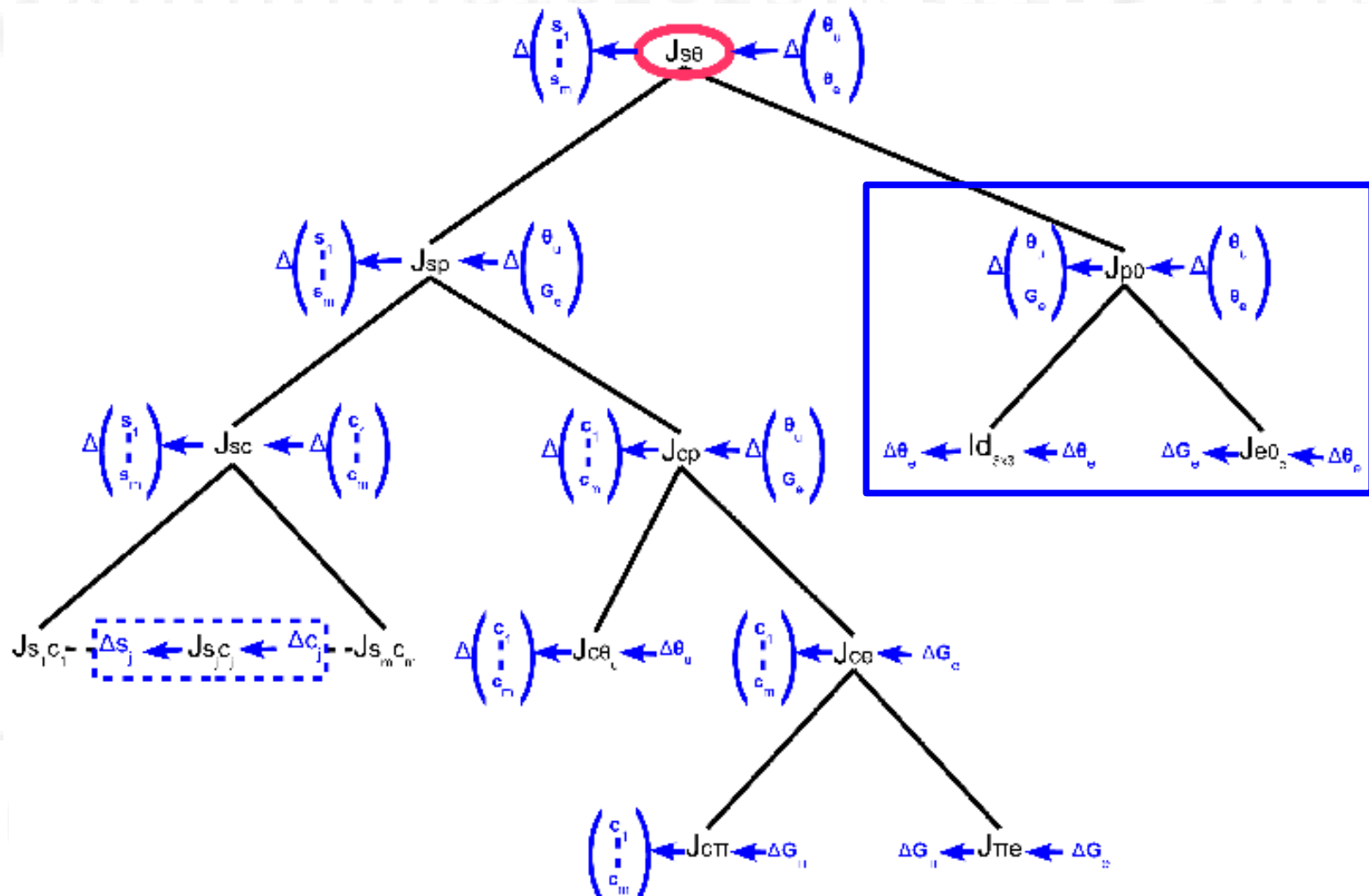


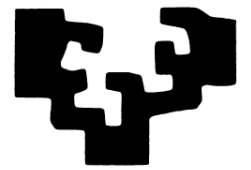


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## Direct Kinematics

Structure of direct kinematic function

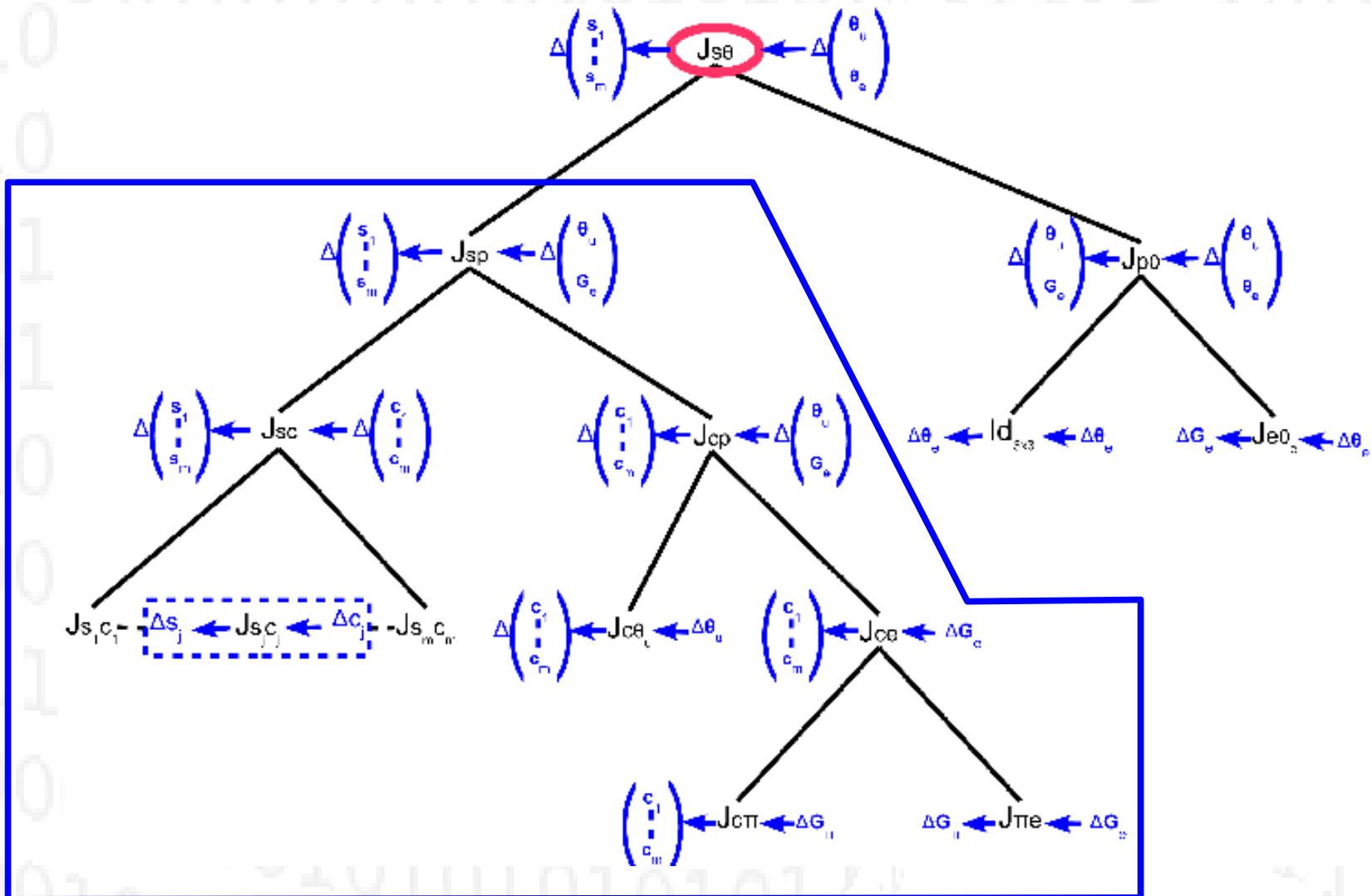




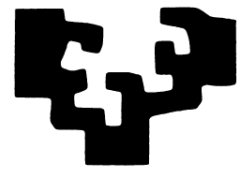
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## Direct Kinematics

Structure of direct kinematic function



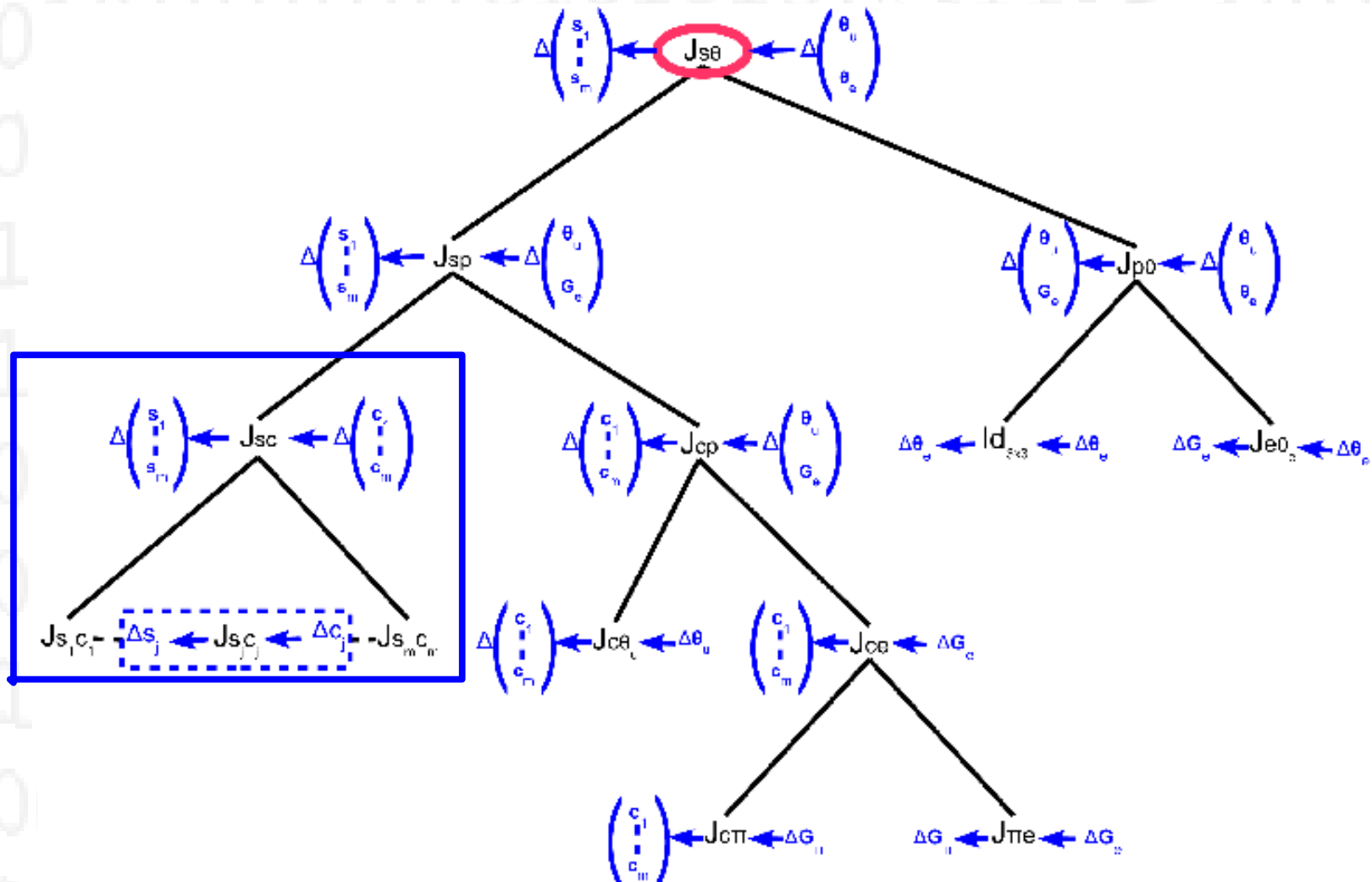


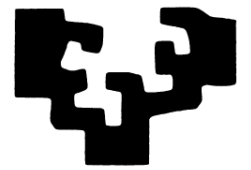


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## Direct Kinematics

Structure of direct kinematic function

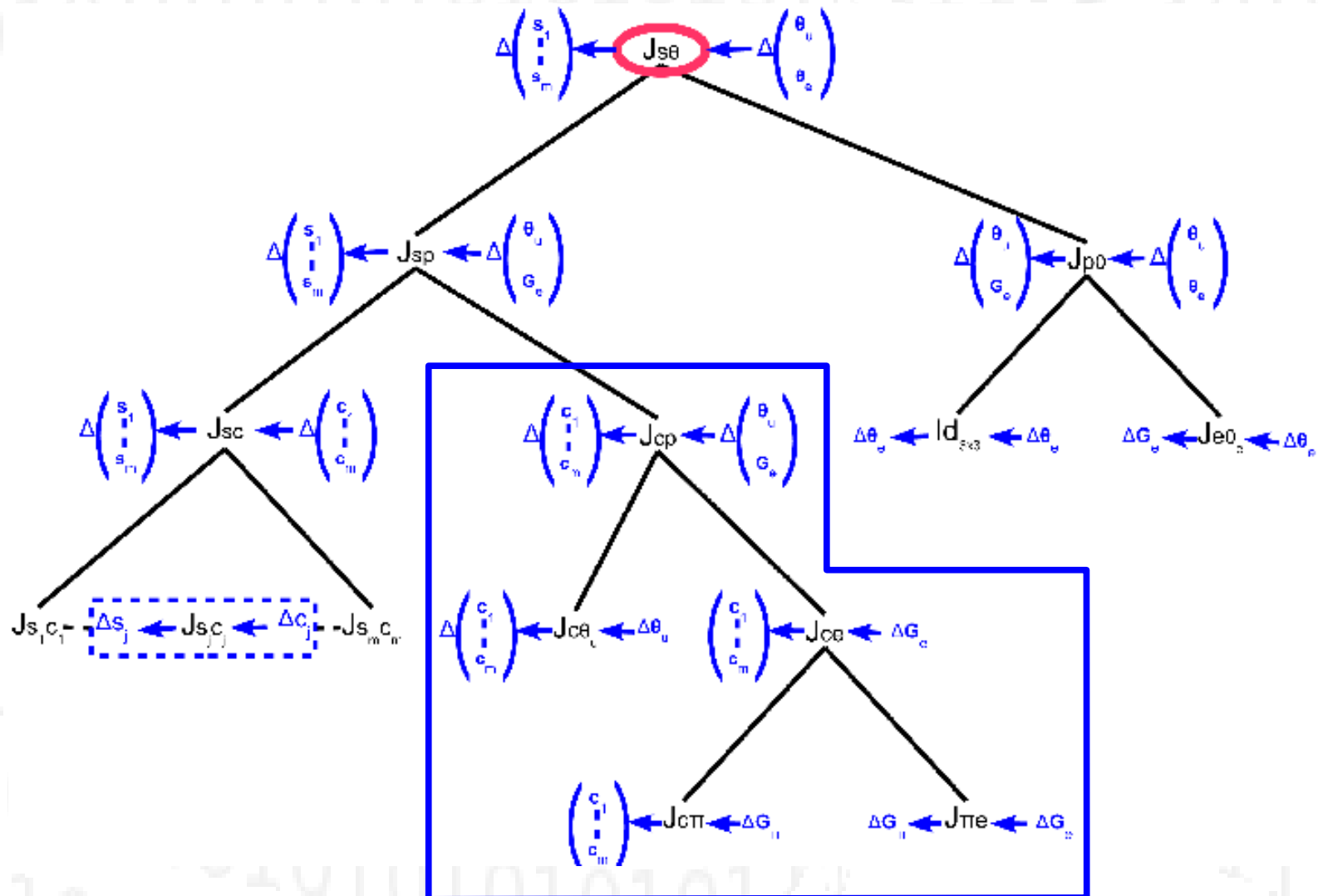


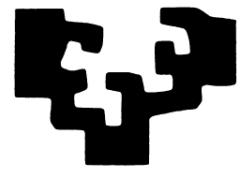


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## Direct Kinematics

Structure of direct kinematic function





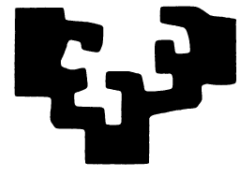
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# Visual Servoing for Legged robots

## Inverse Kinematics



Objective: obtain the joints velocities in order to minimize the norm of the visual error:

$$\min_{\dot{\theta}} \|s^* - (s + J_{s\theta} \dot{\theta})\|$$

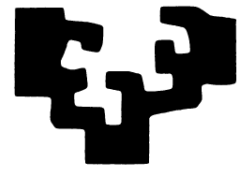
Restriction: keep the support points fixed on the ground

We try to maintain the distances between support points constant



# Visual Servoing for Legged robots

## Inverse Kinematics



### Keeping the supporting points fixed on the ground

Distance between support points

$$\mathbf{d} = \begin{pmatrix} d_1 \\ \vdots \\ d_{n(n-1)} \end{pmatrix}$$



$$\mathbf{J}_{de} =$$

$$\begin{pmatrix} \frac{\partial d_1}{\partial \mathbf{e}_1} & \cdots & \frac{\partial d_1}{\partial \mathbf{e}_n} \\ \vdots & \ddots & \vdots \\ \frac{\partial d_n}{\partial \mathbf{e}_1} & \cdots & \frac{\partial d_n}{\partial \mathbf{e}_n} \end{pmatrix}$$

Jacobian of  $\mathbf{d}$

Extending the sensitivity to upper joints

$$\mathbf{J}_{dp} = \begin{pmatrix} \mathbf{O}_{n \times m} & \mathbf{0} \\ \mathbf{0} & \mathbf{J}_{de} \end{pmatrix}$$

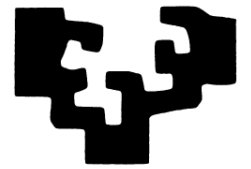


$$\Delta \mathbf{d} \approx \mathbf{J}_{dp} \begin{pmatrix} \Delta \boldsymbol{\theta}_u \\ \Delta \mathbf{G}_e \end{pmatrix}$$



# Visual Servoing for Legged robots

## Inverse Kinematics



Control of image features

$$\Delta \mathbf{p}^1 = [(\mathbf{I} - \mathbf{J}_{dp}^+ \mathbf{J}_{dp}) (\mathbf{J}_{sp}^+)] k_s \Delta \mathbf{s}$$

Control of distances between support points

$$\Delta \mathbf{p}^2 = [(\mathbf{I} - \mathbf{J}_{sp}^+ \mathbf{J}_{sp}) (\mathbf{J}_{dp}^+)] k_d \Delta \mathbf{d}$$

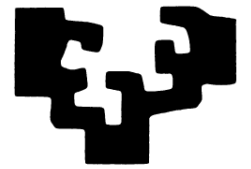
Global control

$$\Delta \boldsymbol{\theta} = \mathbf{J}_{p\theta}^+ \left\{ \Delta \mathbf{p}^1 + \Delta \mathbf{p}^2 \right\}$$

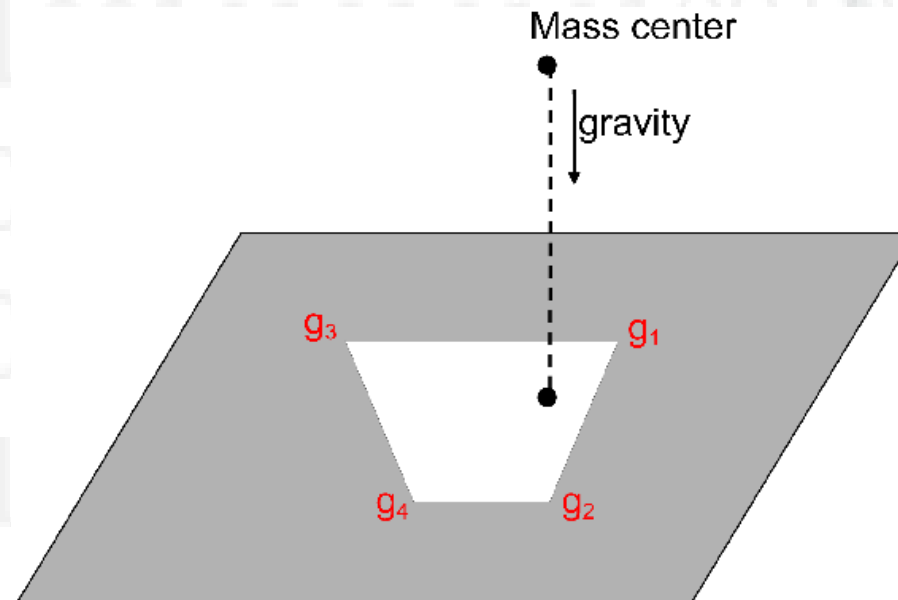


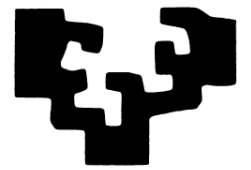
# Visual Servoing for Legged robots

## Inverse Kinematics



- The blind application of this control strategy may lead the robot to unstable configurations for a standing pose.
- When stability is compromised we restrict the Visual Servoing to the upper degrees of freedom.

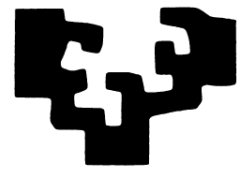




# Outline

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- Visual Servoing general ideas
- **Visual Servoing for legged robots**
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  - Basic problems
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  - Inverse Kinematics
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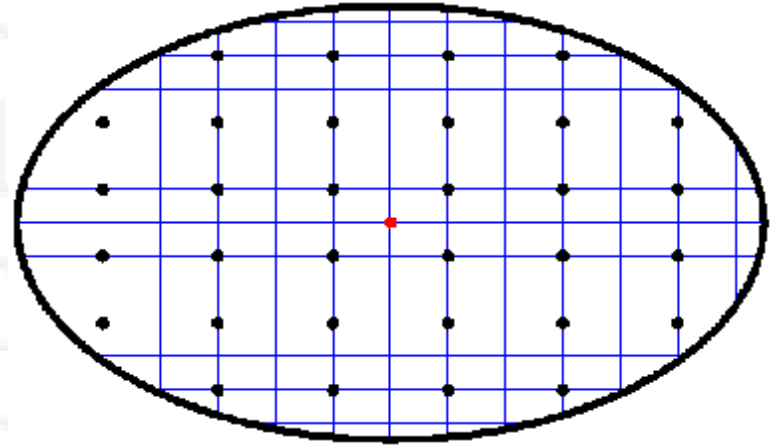
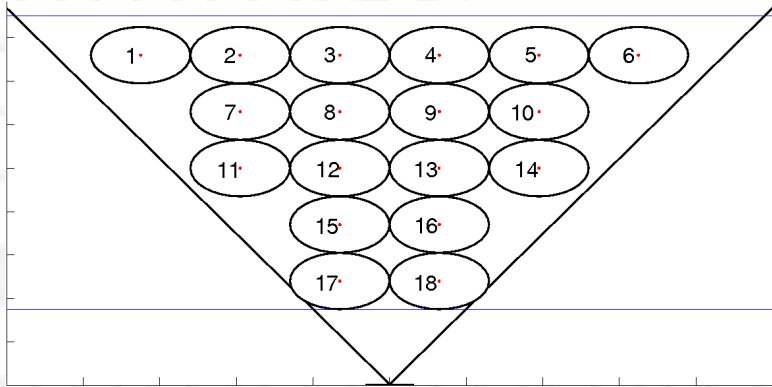


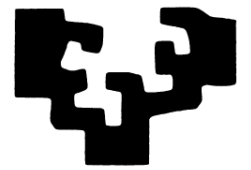


# Visual Servoing for Legged robots

## Experimentation with an Aibo ERS7 robot

### Experiments under controlled conditions

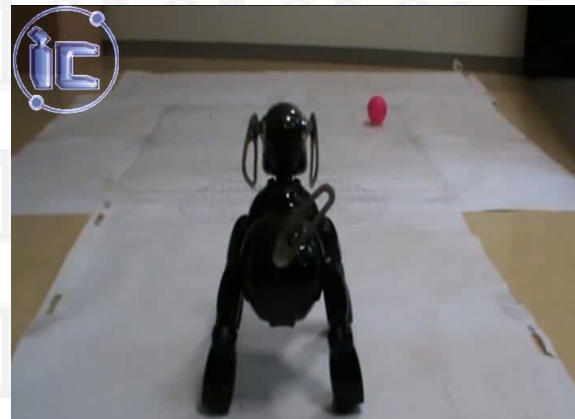


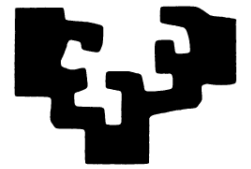


Visual Servoing for Legged robots  
Experimentation with an Aibo ERS7 robot

## Experiments under controlled conditions

Video



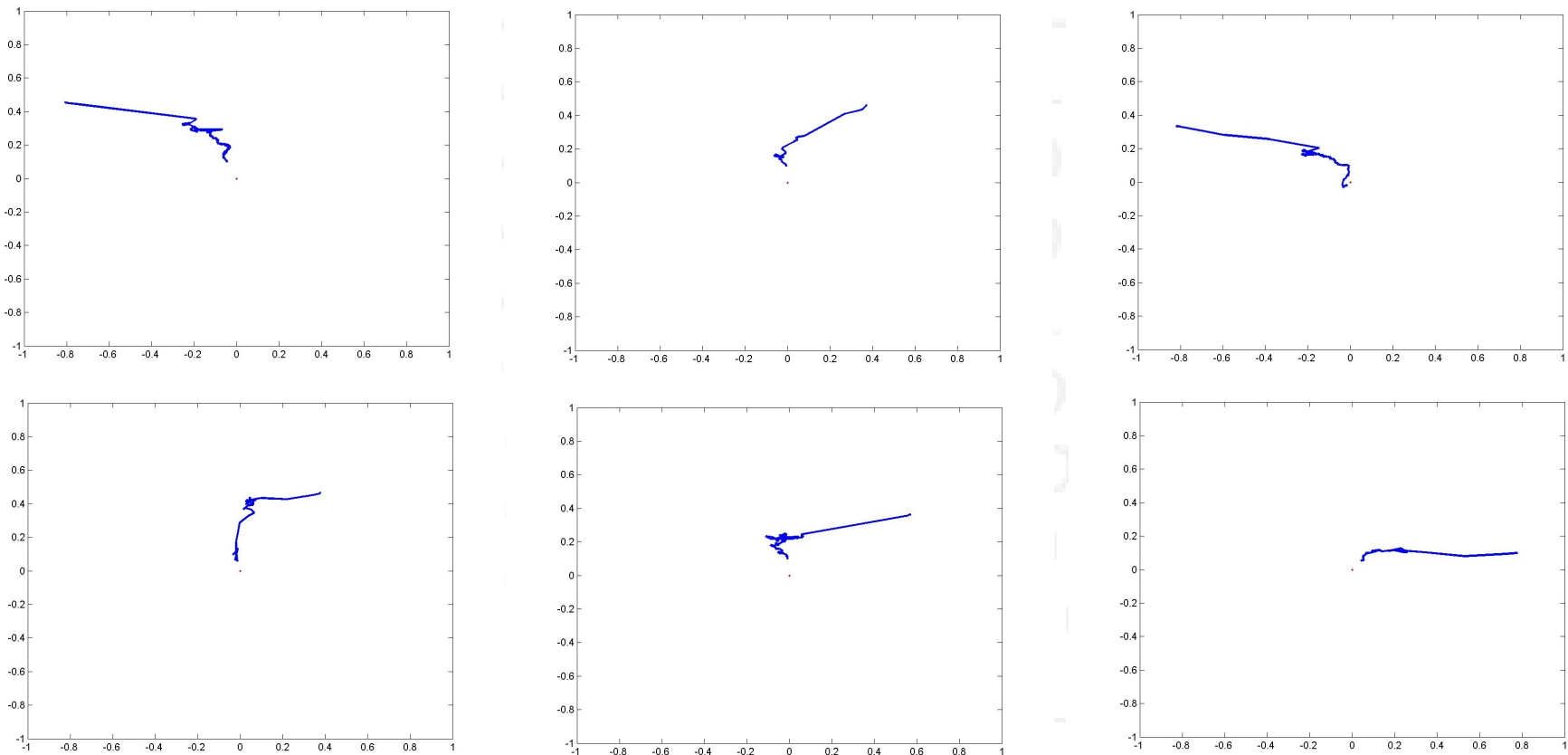


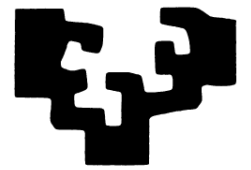
# Visual Servoing for Legged robots

## Experimentation with an Aibo ERS7 robot

### Empirical results

Sample trajectories of the ball center in the image with the ball placed in some position inside the uncertainty circles.



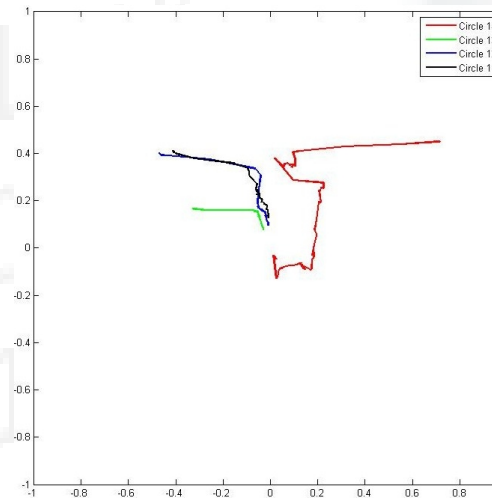
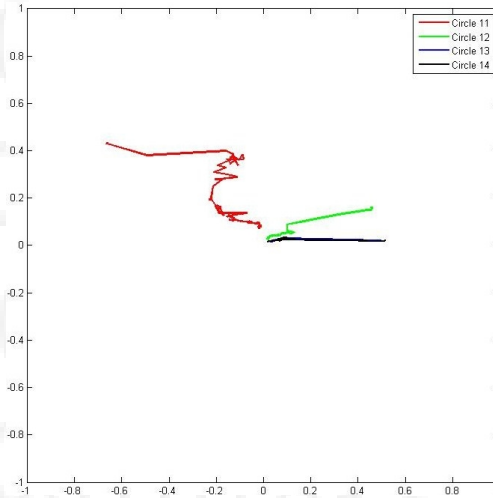
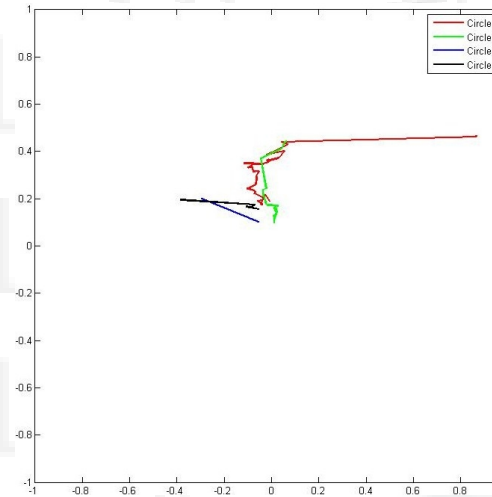
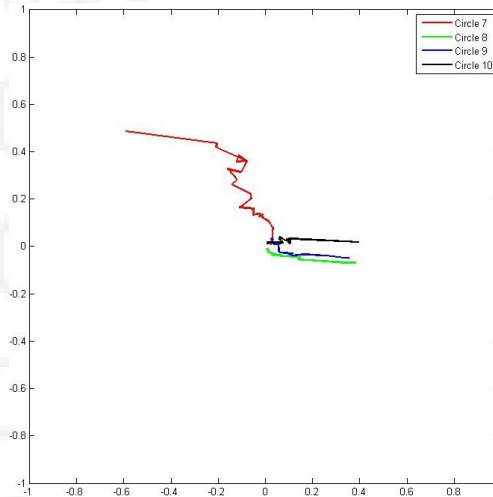


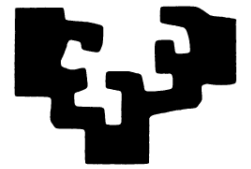
# Visual Servoing for Legged robots

## Experimentation with an Aibo ERS7 robot

### Empirical results

Sample trajectories for a moving ball





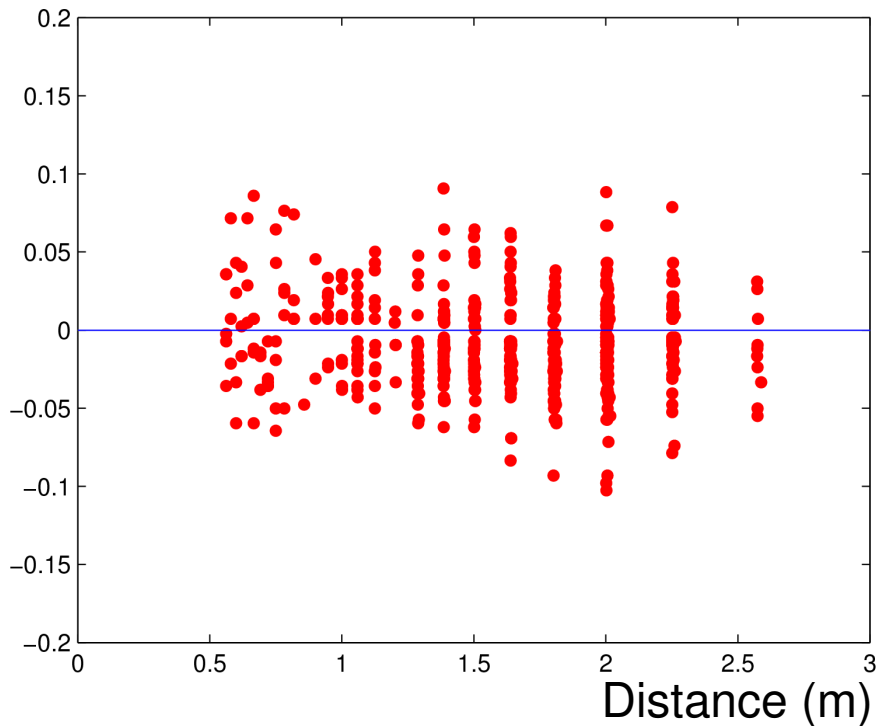
# Visual Servoing for Legged robots

## Experimentation with an Aibo ERS7 robot

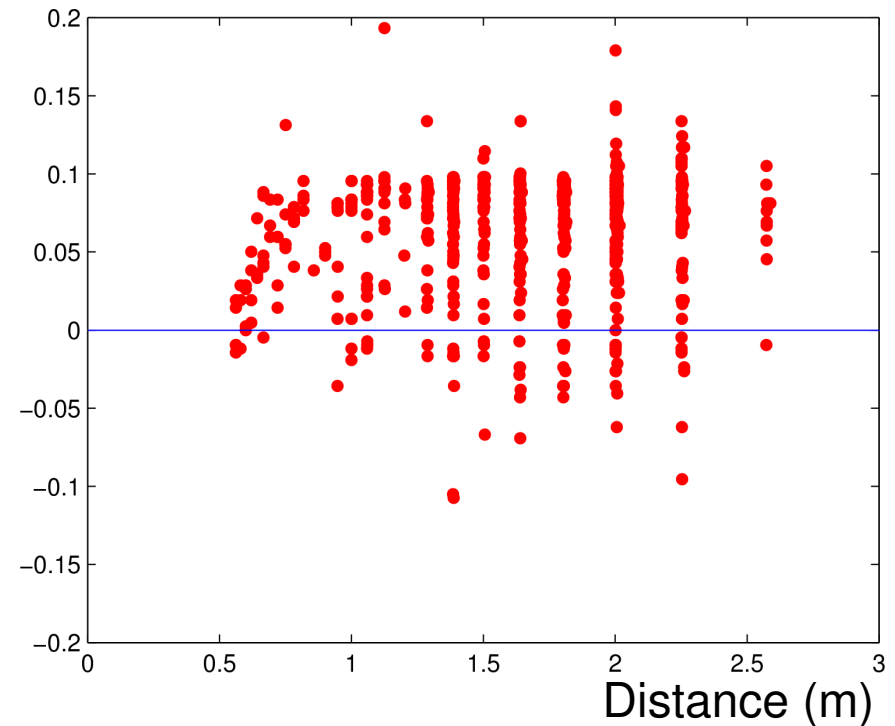
### Empirical results

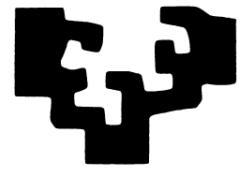
Final error distribution versus 3D distance to the ball

Error in the horizontal axis



Error in the vertical axis





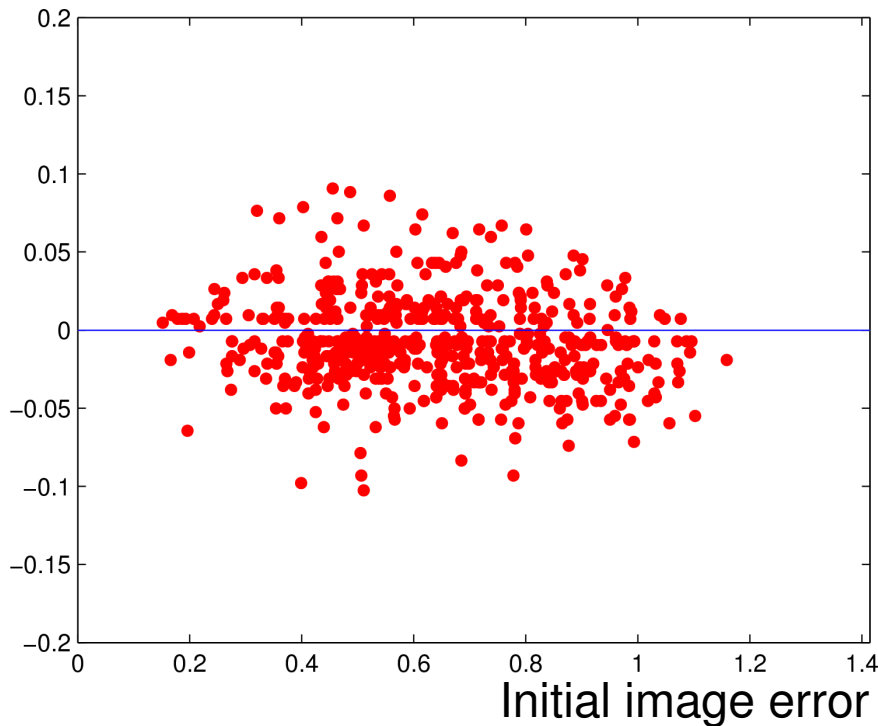
# Visual Servoing for Legged robots

## Experimentation with an Aibo ERS7 robot

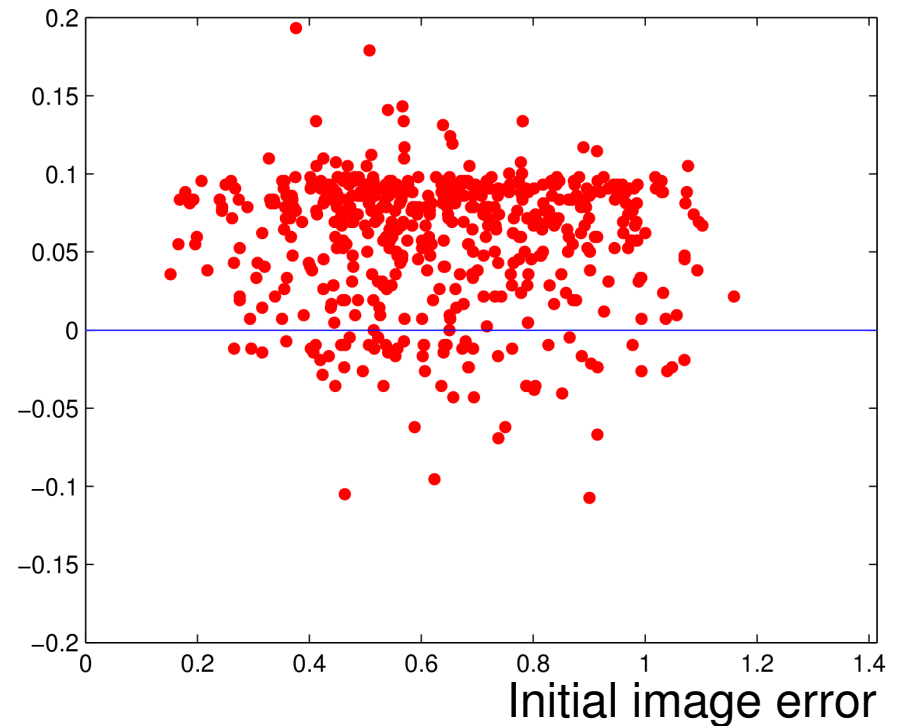
### Empirical results

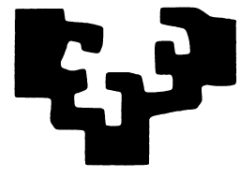
Final error distribution versus initial distance in image plane

Error in the horizontal axis



Error in the vertical axis





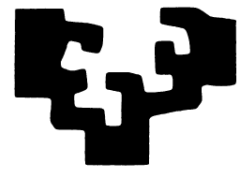
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# Visual Servoing for Legged robots

## Conclusions



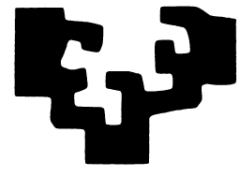
- We have developed a Visual Servoing approach for all the degrees of freedom of a legged robot.
- We have constructed the full Jacobian matrix that linearizes the functional dependence of visual observations by the robot camera on the robot degrees of freedom.





# Visual Servoing for legged robots

## Conclusions

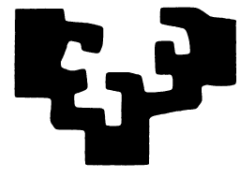


- We have developed a physical realization on the Aibo ERS7 robot.
- The approach obtains the desired control commands.
- The approach performs in real time in the on-board processor of the robot.
- The approach is highly robust to positioning of the ball in the field of view of the robot.
- Very low final error, whose distribution is invariant to the distance of the ball to the camera.



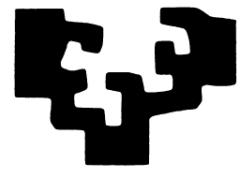
# Visual Servoing for Legged robots

## Conclusions



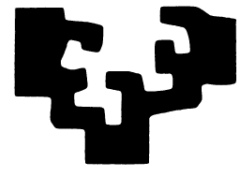
As the main sources of convergence problems we have identified the following ones:

- The linear nature of the approach.
- The resolution and power of the physical servo-motors.
- The problems in the image segmentation.



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# Control of Linked MCRS

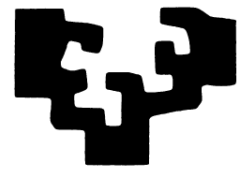
## Motivation

- When a task can not be performed by a single robot, a team of robots may cooperate with each other in order to execute it.
- Categorization of MCRS based on morphological features by Duro et al.:
  - Modular: rigid connections between robots.
  - Distributed: there is no physical union.
  - Linked: the robots are linked by a passive element.
- Linked MCRS is a new category that has not been explored.

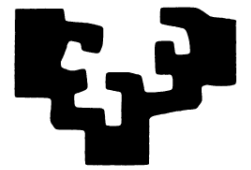


# Control of Linked MCRS

## Objectives



- Obtain a formal model of the Linked MCRS, for the transport of a hose, from a geometrical and dynamical point of view.
- The model could be easily adapted to new instances of the system, varying the parameters of the linking element and/or the individual robots.
- This model would be used to:
  - Simulate the system.
  - Test heuristics and control strategies.
- Derive control strategies from the analytical model.
- Demonstrate empirically the fundamental differences between Distributed and Linked MCRS.



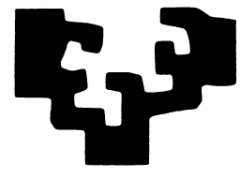
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# Control of Linked MCRS

## Linking element model

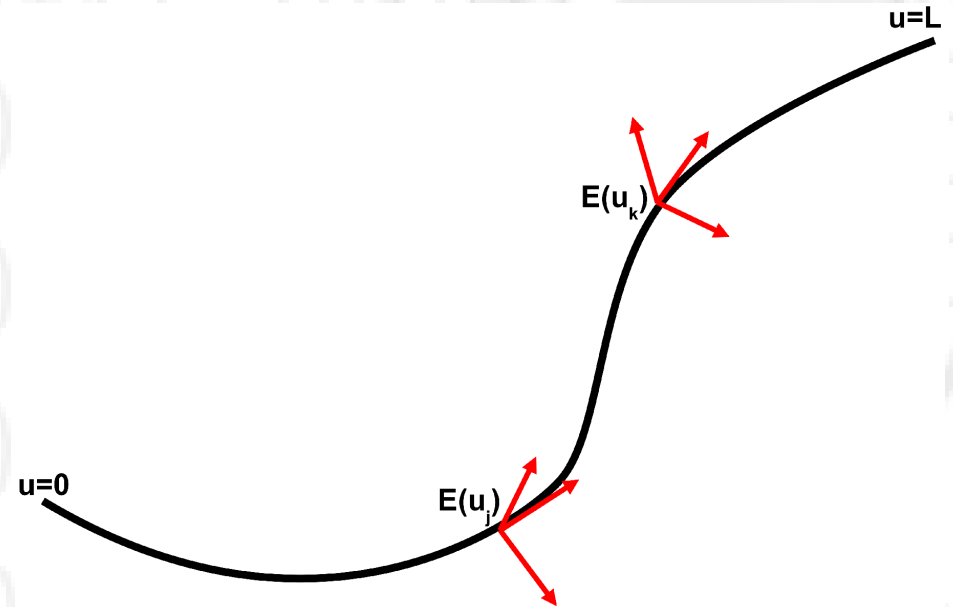


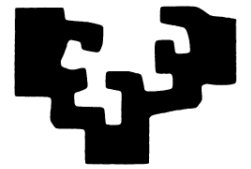
### Cosserat rod theory

An uni-dimensional object is described by a curve  $r(u)$  and a coordinate frame of director vectors  $[e_1, e_2, e_3](u)$  attached to each point of the curve.

$$E(u) = [e_1, e_2, e_3, r](u)$$

$$u \in [0, L]$$





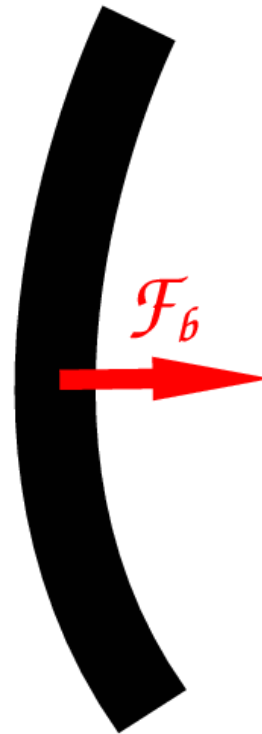
# Control of Linked MCRS

## Linking element model

### Forces induced by the potential energy of the hose



Stretching force



Bending force



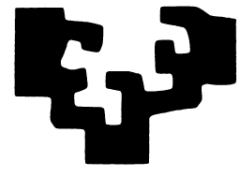
Twisting force



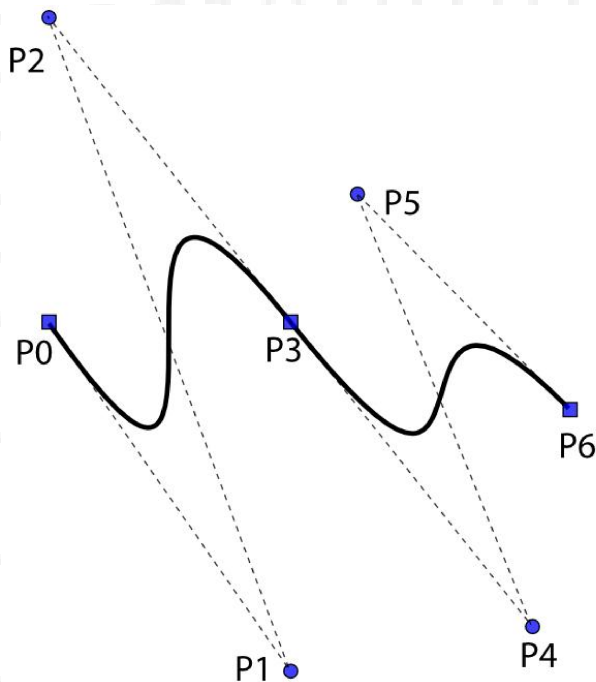


# Control of Linked MCRS

## Linking element model

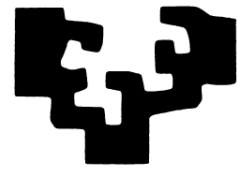


### Dynamic splines



$$\mathbf{q}(u, t) = \sum_{i=0}^n N_i(u) \cdot \mathbf{p}_i(t)$$

Problems with splines model: Are based on the control points of the spline, therefore they are not suitable for representing the hose torsion.

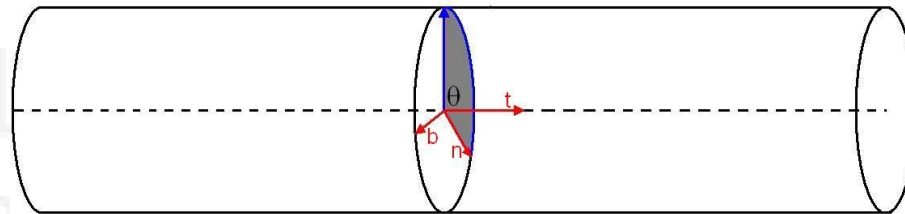


# Control of Linked MCRS

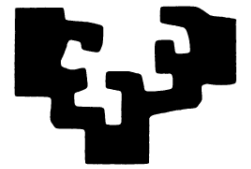
## Linking element model

### Geometrically Exact Dynamic Splines (INRIA 2006)

GEDS takes into account the torsion by using a fourth component in the control points.



$$p_i = (x_i, y_i, z_i, \theta_i)$$



# Control of Linked MCRS

## Linking element model

### Energy formulation

Potential energy

$$U = \frac{1}{2} \cdot \int_0^L \epsilon^t H \epsilon du$$

$$H = \begin{pmatrix} E_s & 0 & 0 \\ 0 & E_t & 0 \\ 0 & 0 & E_b \end{pmatrix}$$

$E_s$  Stretching deformation

$E_t$  Twisting deformation

$E_b$  Bending deformation

Kinetic energy

$$T = \frac{1}{2} \cdot \int_0^L \frac{d\mathbf{q}^t}{dt} J \frac{d\mathbf{q}}{dt} du$$

$$J = \begin{pmatrix} \mu & 0 & 0 & 0 \\ 0 & \mu & 0 & 0 \\ 0 & 0 & \mu & 0 \\ 0 & 0 & 0 & I \end{pmatrix}$$

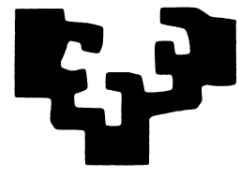
$\mu$  Linear density

$I$  Polar momentum of inertia



# Control of Linked MCRS

## Linking element model



### Dynamics

We want to obtain the forces that robot must apply to obtain in order to approximate the desired acceleration of the hose

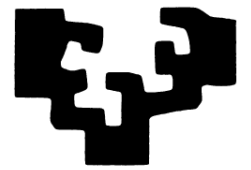
### Lagrange equation

$$\frac{d}{dt} \left( \frac{\partial T}{\partial \dot{\mathbf{p}}_i} \right) = \mathbf{F}_i - \frac{\partial U}{\partial \mathbf{p}_i}$$

Defines a mathematical relation between:

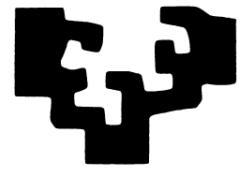
- U, potential energy.
- T, kinetic energy.
- F, external forces.

$$\mathbf{M} \mathbf{A} = \mathbf{F} + \mathbf{P}$$



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# Control of Linked MCRS

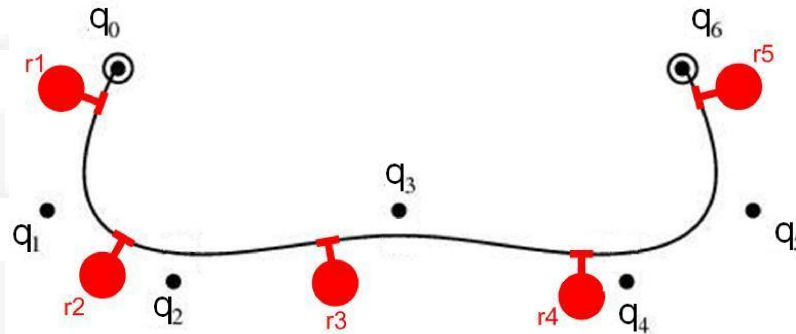
## Linked MCRS configuration

### Configuration defined by B-splines

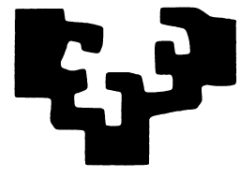
$$h = [p, U, U_r]$$

where:

- $p$  is the control point vector of the hose B-spline model.
- $U$  is the vector of knots in the B-spline model.
- $U_r$  is the robots knot vector.



$$q(u_{r_i}) = \sum_{i=0}^n N_i(u_{r_i}) \cdot p_i = r_i, \forall i \in [0, L]$$



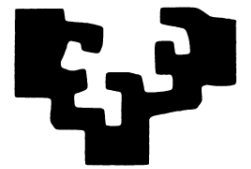
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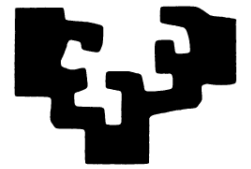
# Control of Linked MCRS

## Linked MCRS control



- We define two basic kinds of hose positioning task:
  - Bring the hose from an initial configuration to a final configuration.
  - Given a sequence of hose configurations, the system must follow it in order to accomplish the transport of the hose.





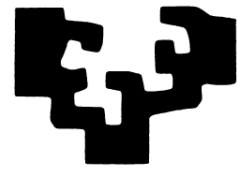
# Control of MCRS

## Linked MCRS control

### Transitions among configurations

We want to obtain the motion of the attached robots which will move the hose from the initial hose configuration to the desired configuration.

$$p_0 \longrightarrow p_*$$



# Control of Linked MCRS

Linked MCRS control

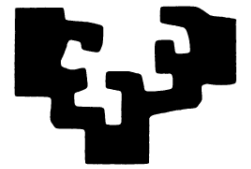
## Transitions among configurations

Configuration error

$$e(\mathbf{p}) = (\mathbf{p}_* - \mathbf{p})^2$$

Proportional control law on the control points

$$\dot{\mathbf{p}} = k(\mathbf{p}_* - \mathbf{p})$$



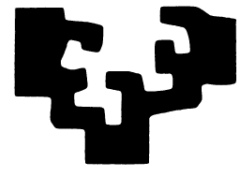
# Control of Linked MCRS

## Linked MCRS control

### Transitions among configurations

- We derive the control points velocities and use the desired control points accelerations in the matricial Lagrange equation in order to obtain the required external forces  $F$  that robots must generate in the control points.

$$\widehat{F}_p = M \widehat{A} - P - F_e$$



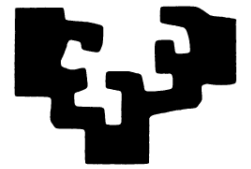
# Control of Linked MCRS

## Linked MCRS control

### Transitions among configurations

- From an inversion of the hose model we obtain the forces that robot must exert  $F_r$  in order to obtain the required external forces in the control points  $F_p$ .

$$\hat{F}_r = J_{pr}^+ \cdot F_p$$



# Control of Linked MCRS

## Linked MCRS control

### Transitions among configurations

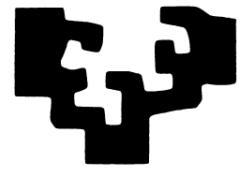
- Applying the obtained robot forces in the direct model we obtain the control points accelerations  $\hat{A}$ .

$$M \hat{A} = F_e + P + J_{pr} \cdot \hat{F}_r$$

- Then we obtain the robots accelerations

$$\hat{A}^r = J_{pr} \cdot \hat{A}$$

- Finally, integrating the robots' accelerations  $\hat{A}^r$  we obtain the robots velocities.



# Control of Linked MCRS

## Linked MCRS control

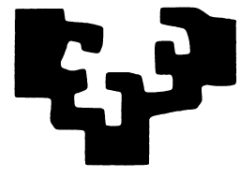
### Following a sequence of intermediate configurations

We interpolate the sequences of configurations  $\mathbf{h}_k$  by a clamped B-interpolating curve

$$\boldsymbol{\phi}(\xi), \xi \in [0, 1] \quad \boldsymbol{\phi}(0) = \mathbf{p}_0, \boldsymbol{\phi}(1) = \mathbf{p}_*$$

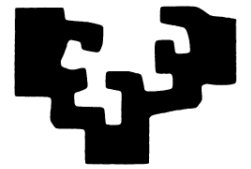
We follow continuously the interpolating curve by a mean velocity close to  $\mathbf{v}_{ref}$ .

$$\dot{\mathbf{p}} = k \cdot [\boldsymbol{\phi}(f(\mathbf{v}_{ref}, \mathbf{p})) - \mathbf{p}]$$



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# Control of Linked MCRS

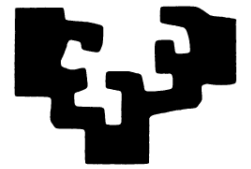
## Linked MCRS control heuristic

### **Follow the leader approach**

From a given trajectory for the leader robot the remaining of the robots must follow it in order to accomplish the transport of the hose.

- We accomplish this task by taking into account:
  - The passive element state (curvature of the hose segments).
  - The distances between consecutive robots.
- In order to define the heuristic, we make the following assumptions:
  - If a pair of robots are too close, the hose segment between them will describe a curve.
  - If a pair of robots are sufficiently separated, the hose is stretched and approximated to the straight line between the robots.





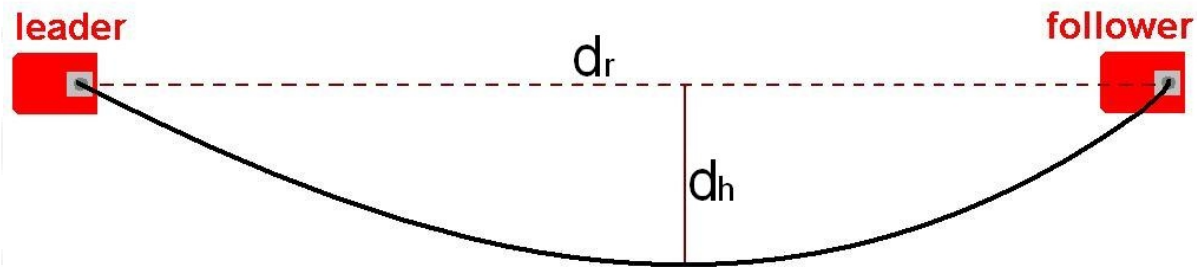
# Control of Linked MCRS

## Linked MCRS heuristics

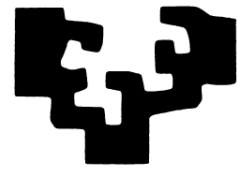
### Follow the leader approach

The curvature of a hose segment is indirectly measured as:

$$c = \frac{d_h}{d_r}$$



We define a maximum  $\bar{c}$  and minimum  $\underline{c}$  segment curvature for the transport of the hose and three speed levels  $w_1$ ,  $w_2$  and  $w_3$ .



# Control of Linked MCRS

## Linked MCRS heuristics

### Follow the leader approach

Rules for determining the robots speed

if  $c_i < \underline{c}$  then

$$w_{i+1} = w_2$$

else

if  $c_i > \bar{c}$  then

$$w_{i+1} = w_0$$

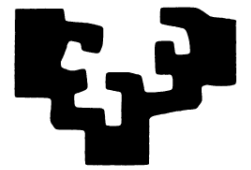
else

$$w_{i+1} = w_1$$



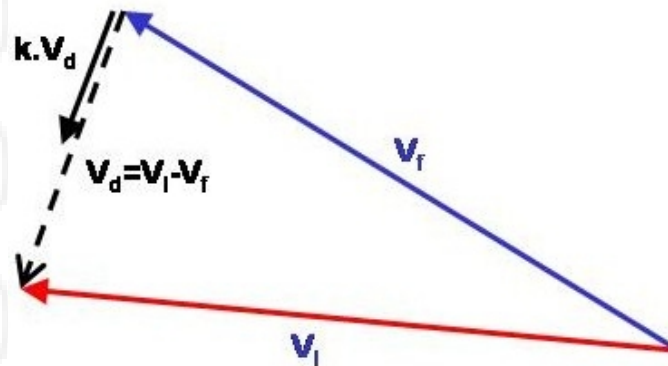
# Control of Linked MCRS

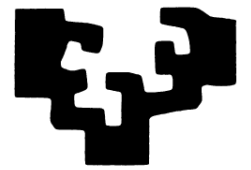
## Linked MCRS heuristics



### Follow the leader approach

Robots' orientation



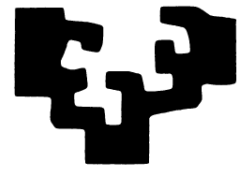


# Outline

- Introduction
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- Visual Servoing for legged robots
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  - Linked MCRS heuristics
  - **Simulation**
  - Real life experimentation
  - Conclusions
- Conclusion

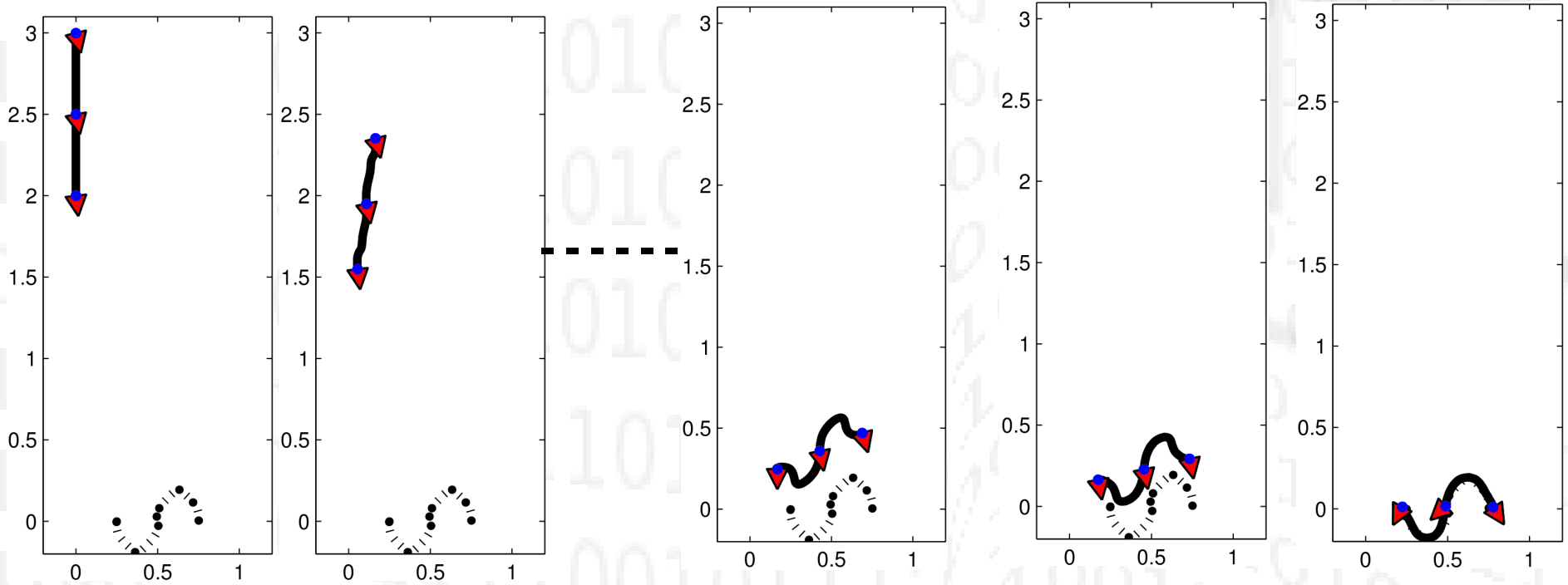


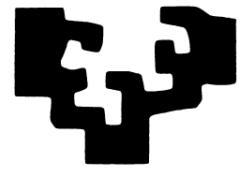
# Control of Linked MCRS Simulation



## Transitions among configurations

Not taking into account the hose dynamics

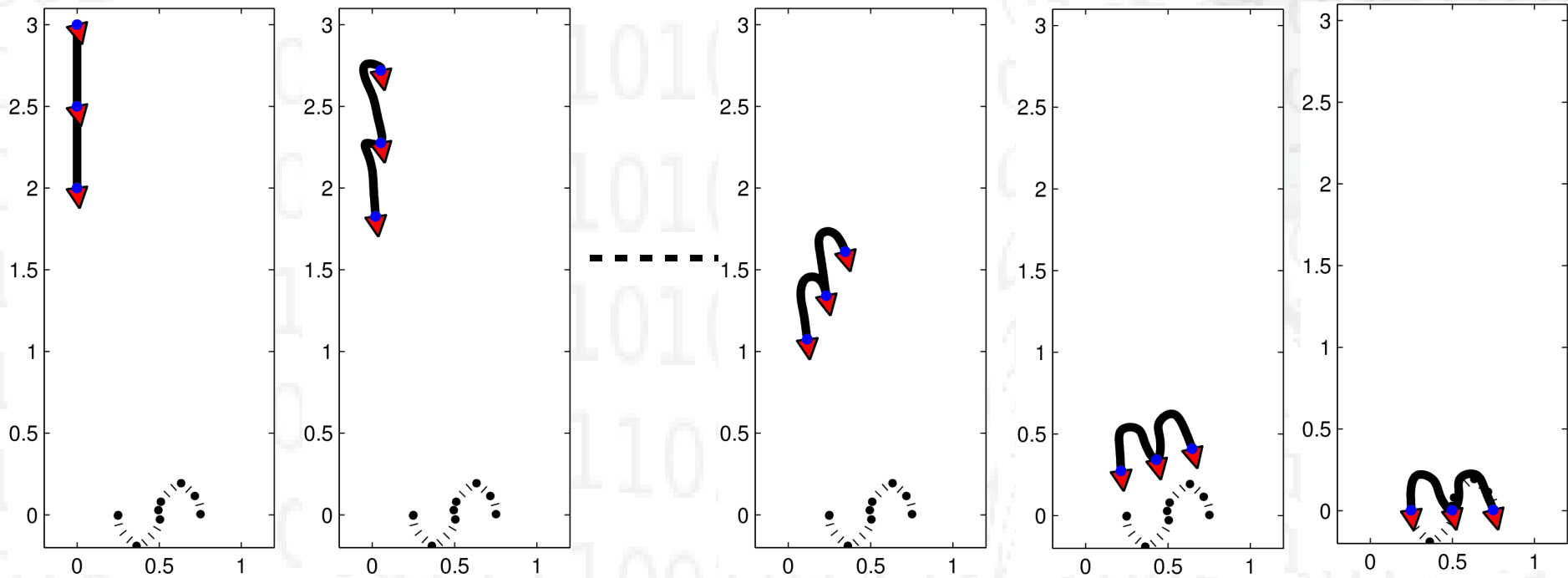




# Control of Linked MCRS Simulation

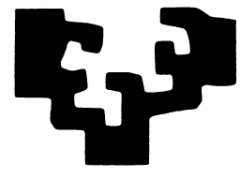
## Transitions among configurations

Taking into account the hose dynamics



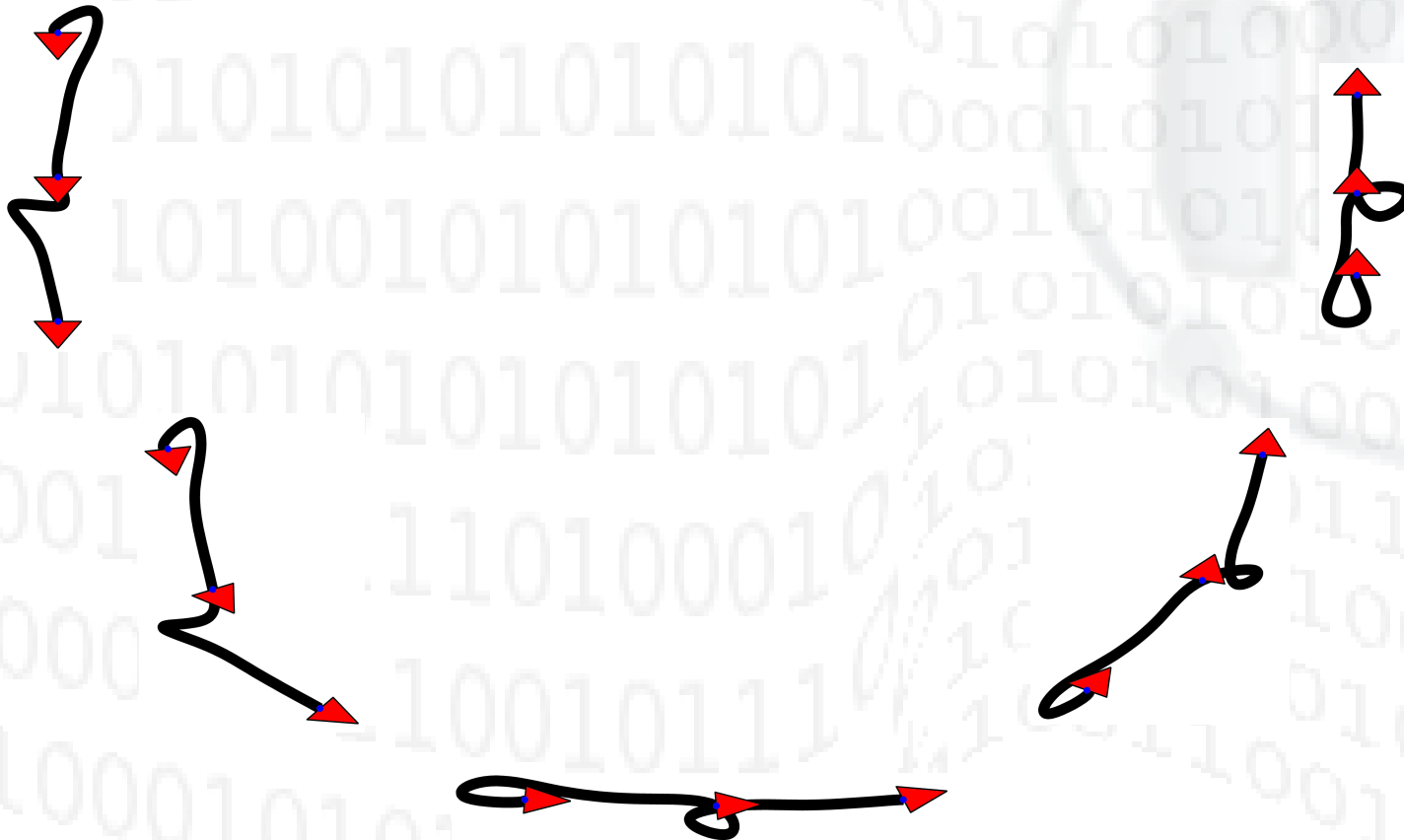


# Control of Linked MCRS Simulation



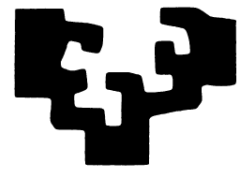
## Hose transportation

Sequence of the trajectory





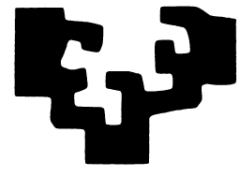
# Control of Linked MCRS Simulation **Video**





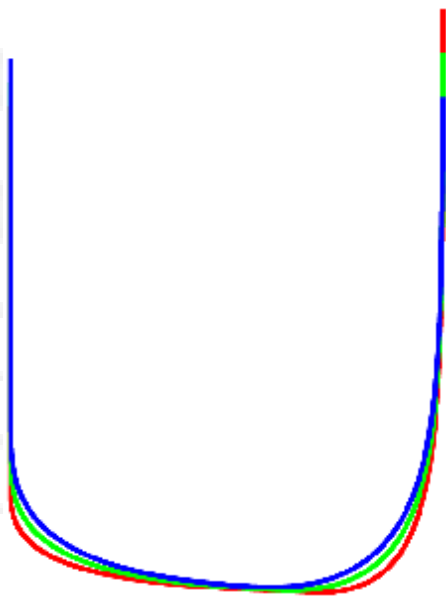


# Control of Linked MCRS Simulation

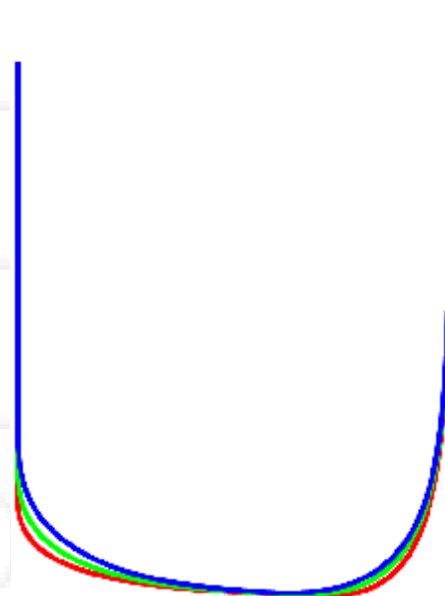


## Hose transportation

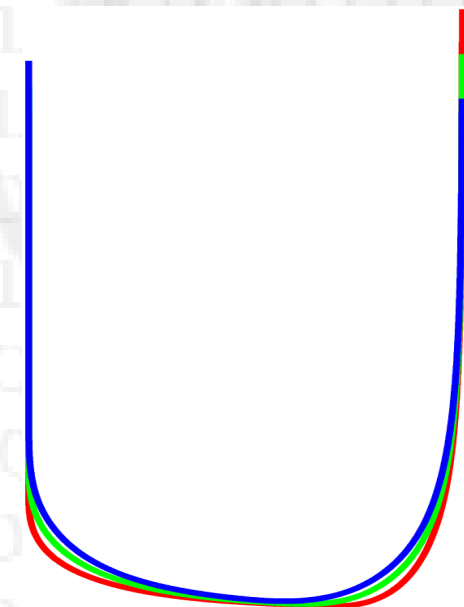
Validation of control approaches



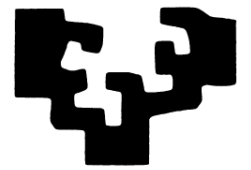
Distance based



Segment based

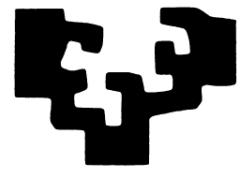


Configuration sequence



# Outline

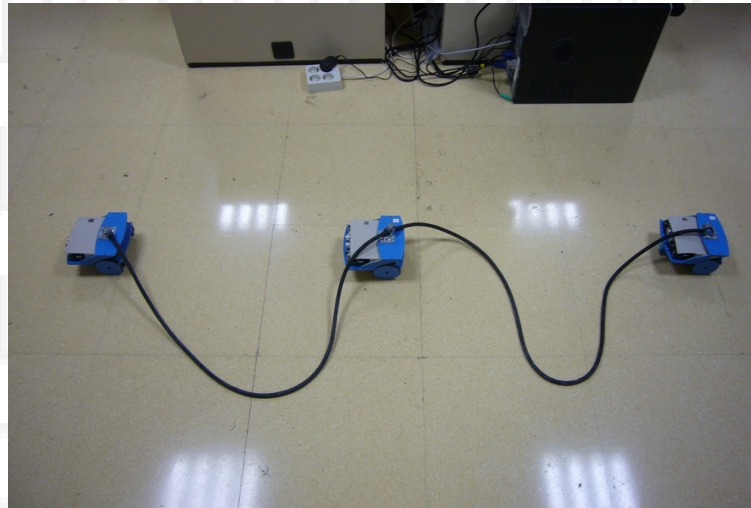
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# Control of Linked MCRS

## Real life experimentation

### Definition

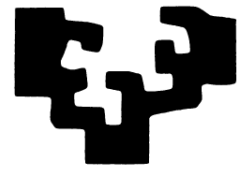


- Basic trajectory for the leader as a straight line.
- Segment curvature based approach.
- Approach to Position based Visual Servoing.
- Fixed camera in a zenith position.
- The Control process is centralized in a master computer.
- Master-slave communication via radio-modems.

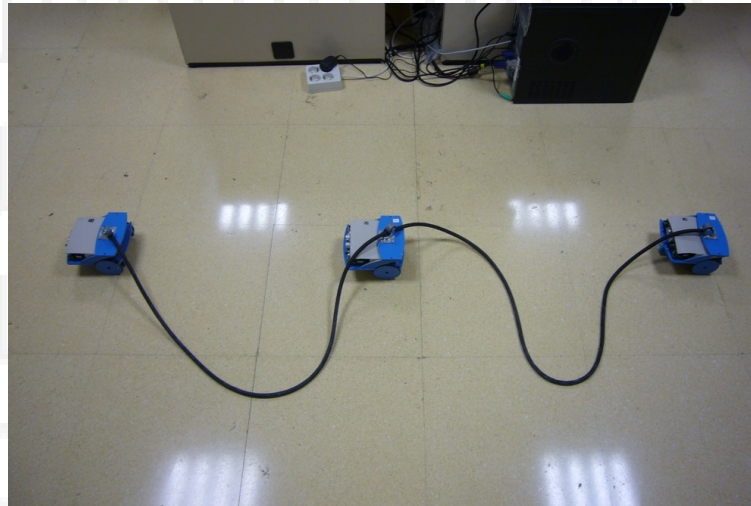


# Control of Linked MCRS

## Real life experimentation



### Starting conditions

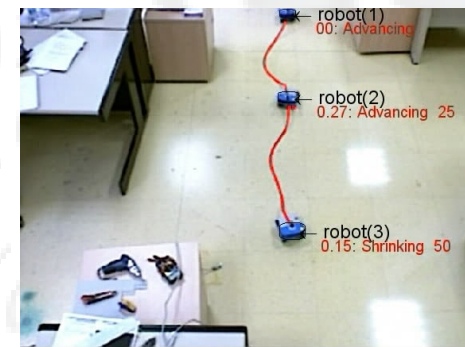
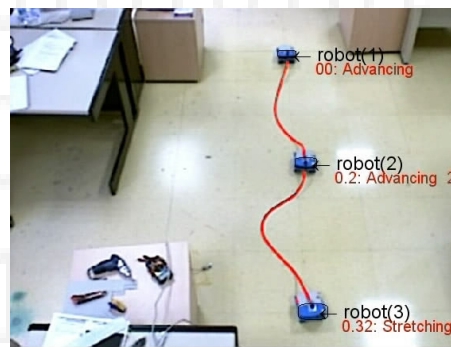
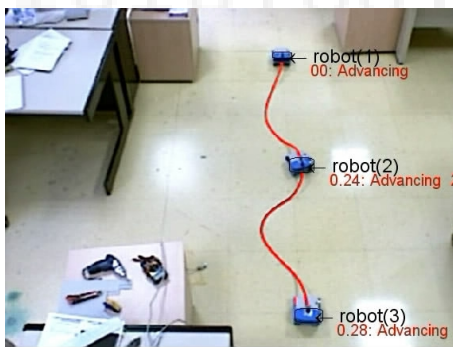
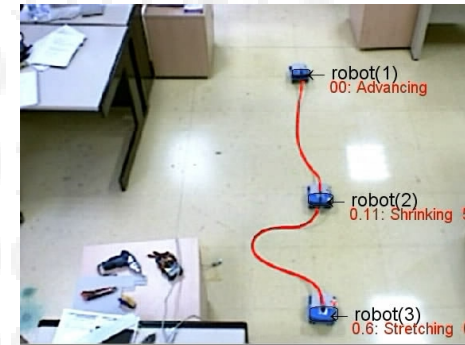
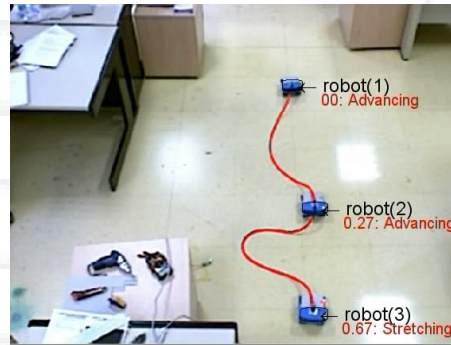
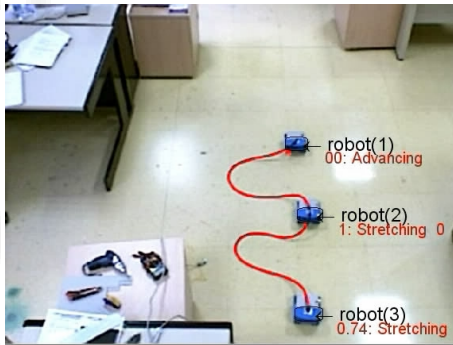
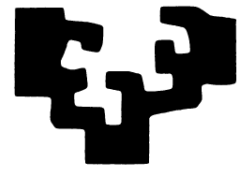


- Hose of 2 meters in length.
  - $\underline{c} = 0.15$
  - $\bar{c} = 0.30$
  - $w_1 = 0$  cm/s
  - $w_2 = 10$  cm/s
  - $w_3 = 20$  cm/s.
- 
- Robots are roughly aligned in the direction of advance.
  - Robots have similar orientations.
  - Hose can be bended but allowing the robots advance.
  - The area in which robots will move must be obstacle free.



# Control of Linked MCRS

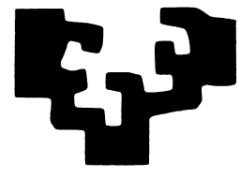
## Real life experimentation



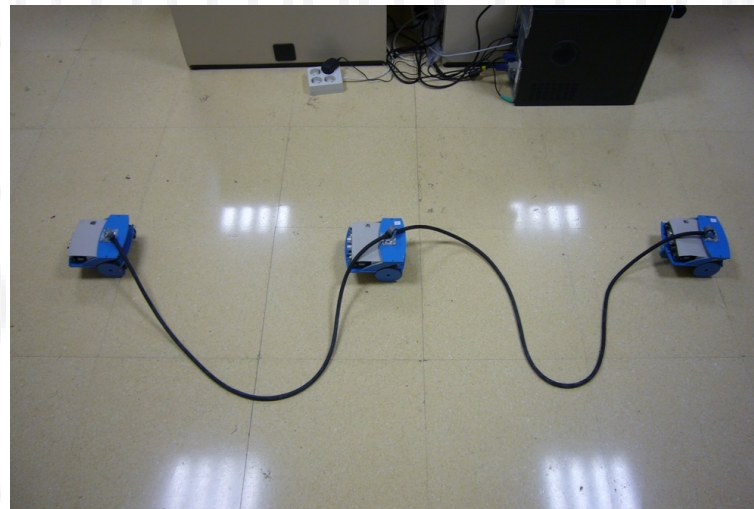


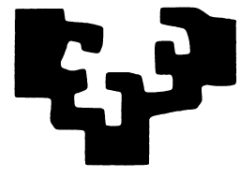
# Control of Linked MCRS

## Real life experimentation



### Video





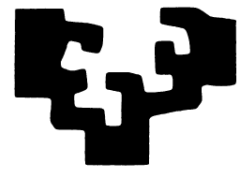
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# Control of Linked MCRS

## Conclusions



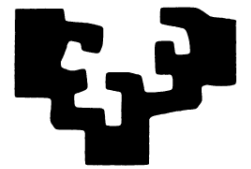
- We have realized a Linked MCRS, opening a whole area of research, showing behaviors that clearly separate it from others kinds of MCRS.
- We have built a geometrical and dynamical model of a Linked MCRS for the transport of a hose, based on the formalism GEDS.
- We have formally derived inverse kinematics/dynamics control rules.





# Control of Linked MCRS

## Conclusions

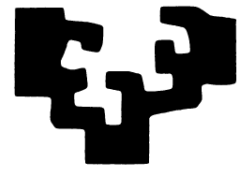


- We have developed a simulation system in order to:
  - Test the formally derived control algorithms.
  - Test heuristic control algorithms.
  - Reproduce some physical phenomena.
- We have built a physical realization of the system, using a centralized Visual Servoing approach.

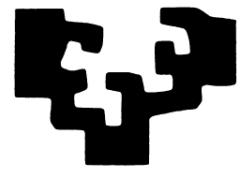


# Control of Linked MCRS

## Conclusions

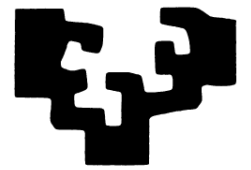


- Future work lines
  - Simulations and physical realization of distributed control approaches.
  - Automated identification of the hose parameters.
  - Solve the problems of local minima for the control of the hose by techniques as Particle filter.



# Outline

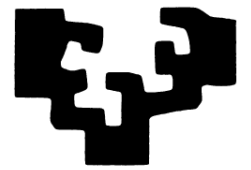
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- **Conclusion**



## Summary of Conclusions

We have worked on visual Servoing applications for two widely different fields of robotics:

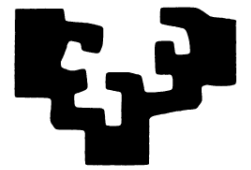
- Legged robots (Aibo):
  - To obtain fast reactive behavior involving all their degrees of freedom.
- Linked Multi Component Robotic Systems:
  - To be able to implement control heuristics on it.



## Summary of Conclusions

For the legged robots (Aibo) we have successfully:

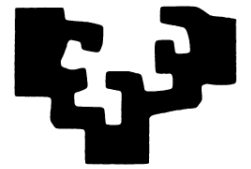
- Formulated a direct kinematics model from its structural description.
- Proposed an inversion model which includes stability constraints.
- Tested empirically the advantages and limitations of the approach.



## Summary of Conclusions

Further work for the legged robots visual servoing:

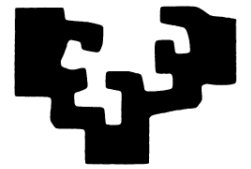
- More extensive experimentation of the real robot.
- Integrate data induction algorithms into the model (Artificial Neural Networks) to improve its robustness.



# Summary of Conclusions

For the Linked MCRS we have successfully

- Proposed a formal direct kinematics model encompassing the passive linking element (the hose).
- Proposed an inversion model that would give the control commands for the robot.
- Perform simulations assessing the expected behavior of the system.
- Test heuristic control strategies:
  - In simulation.
  - On a physical realization.

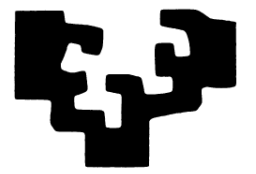


## Summary of Conclusions

Further work on Linked MCRS may address:

- Testing heuristic and formal control approaches under:
  - An extensive simulation exploration of the system's behavior.
  - More extensive physical experiments.
  - Other system embodiments (e-puck robot).





**Thank you for your attention**